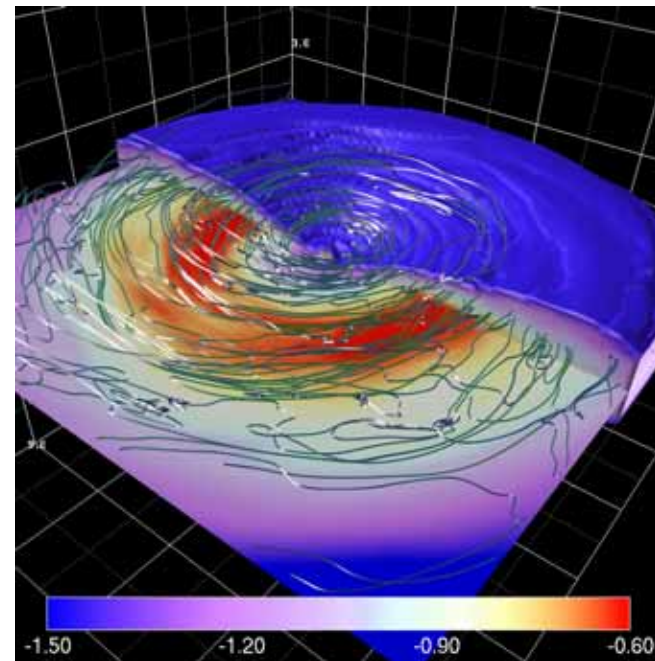
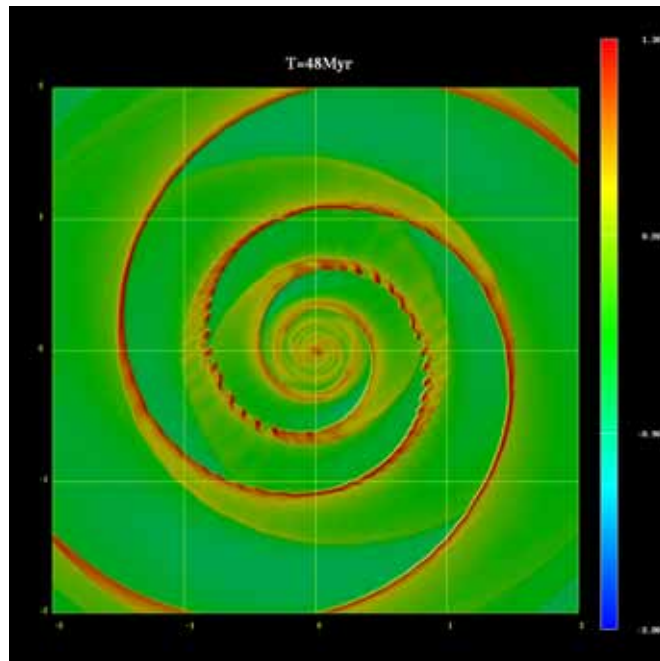
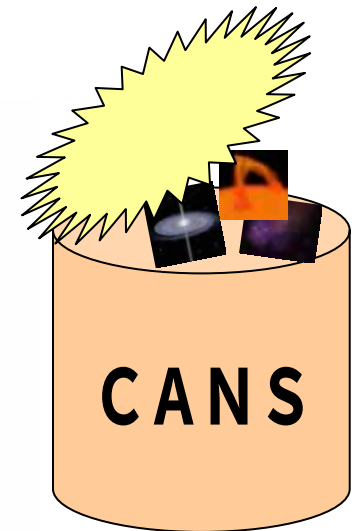
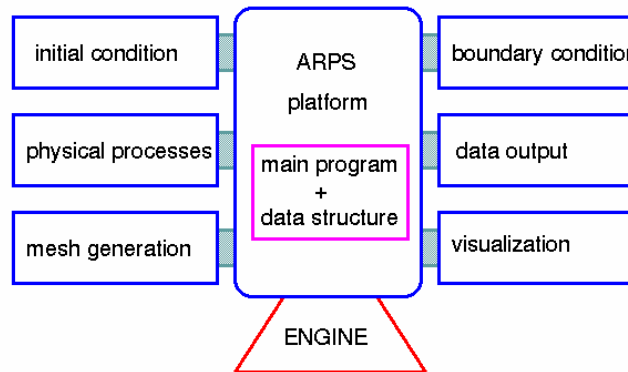


# Global MHD Simulations of Galactic Gas Disks



Ryoji Matsumoto (Chiba University)

# Global Simulators of Astrophysical Rotating Plasmas



ARPS (Astrophysical Rotating Plasma Simulator, Matsumoto et al. 1999)

Coordinated Astronomical Numerical Software(CANS): product of ACT-JST project (2000-2002)

# Basic Equations

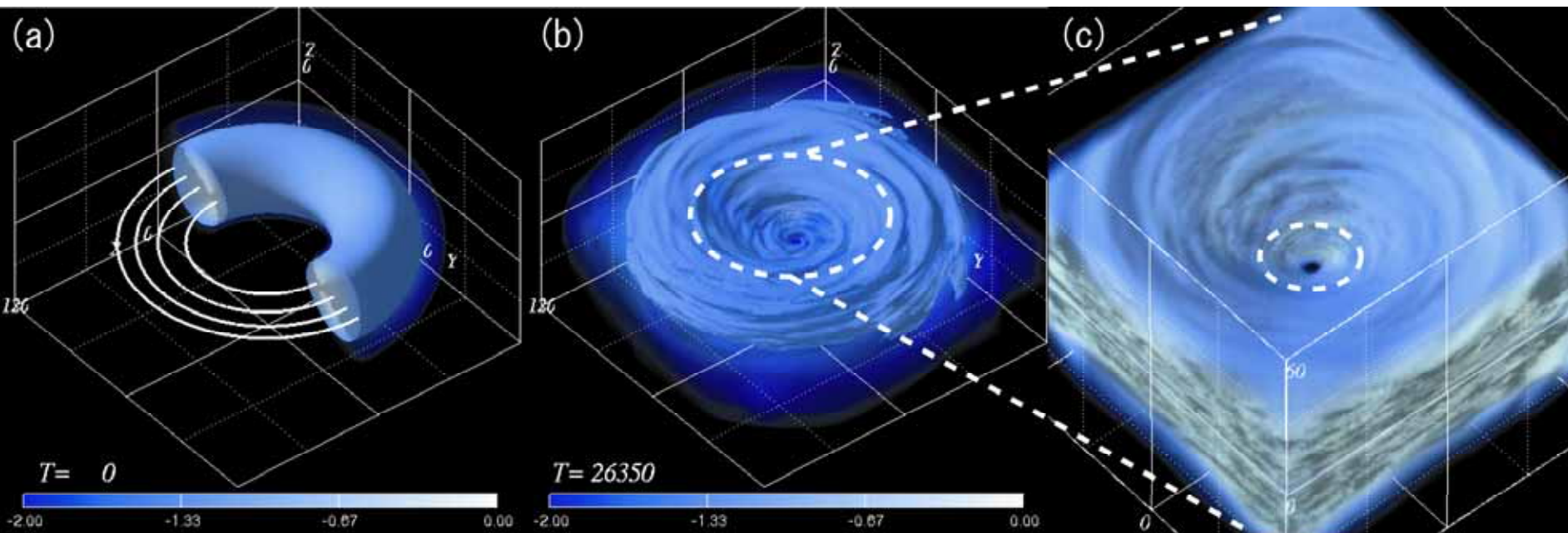
$$\frac{\partial \rho}{\partial t} + \nabla(\rho \mathbf{v}) = 0$$

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho(\mathbf{v} \bullet \nabla) \mathbf{v} = -\nabla P + \frac{(\nabla \times \mathbf{B}) \times \mathbf{B}}{4\pi} + \rho \mathbf{g}$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

$$\frac{\partial \rho \varepsilon}{\partial t} + \nabla(\rho \varepsilon \mathbf{v}) + P \nabla \mathbf{v} = Q_J + Q_{vis} - Q_{rad}$$

# Formation of an Accretion Disk



Initial state

$t=26350$

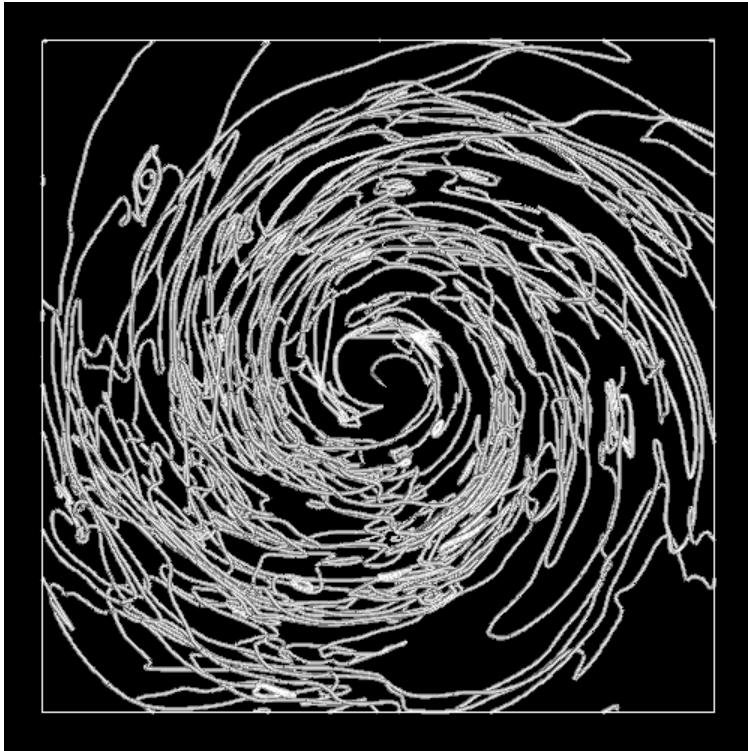
unit time  $t_0=rg/c$



# Magnetic Field Lines

Magnetic field lines projected onto the equatorial plane

$(-60 < x, y < 60)$



Outer region

$(-10 < x, y < 10)$



Inner region

Magnetic field lines are tightly wound.  
⇒ Turbulent motions are dominant in the disk.

Magnetic field lines are less turbulent and globally show bisymmetric spiral shape (BSS).

# Outline of this Talk

- MHD Simulations of the wiggle instability in Galactic gas disks (M. Tanaka, M. Machida, K. Wada and R. Matsumoto 2005)
- Global 3D MHD Simulations of Galactic gas disks (H. Nishikori, M. Machida and R. Matsumoto 2005)



# MHD Simulations of the Wiggle Instability in Galactic Gas Disks



Dark spur-like structures exist perpendicular to the spiral arms

By carrying out 2D global hydrodynamic simulations, Wada and Koda (2003) found that spur-like structures are created behind the spiral shock

# Global Simulations of the Wobble Instability

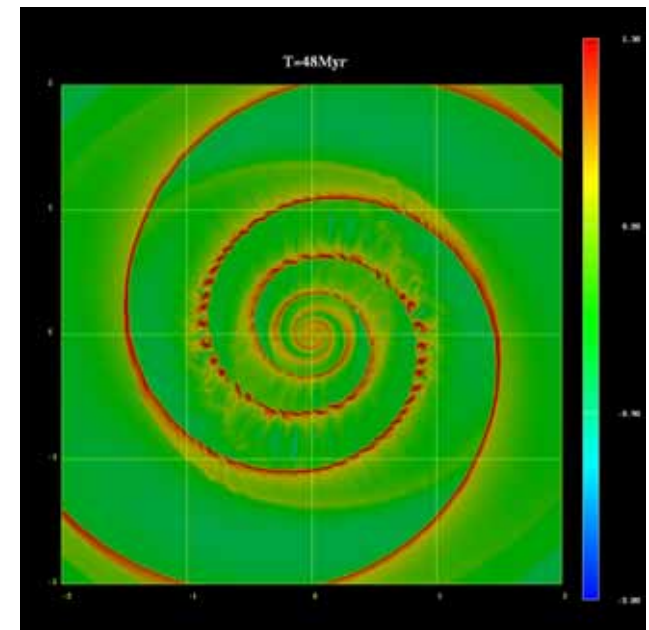
- Gravitational Potential

$$\Phi(r, \phi) \equiv \Phi_0(r) + \Phi_1(r, \phi)$$

$$\Phi_0(r) \equiv av_a^2 \left( \frac{27}{4} \right)^{1/2} (r^2 + a^2)^{-1/2}$$

$$\Phi_1(r, \phi) \equiv \epsilon_0 \frac{ar^2 \Phi_0}{(r^2 + a^2)} \cos[2\phi + 2 \cot i \cdot \ln(r)]$$

- Isothermal gas
- Neglect self-gravity
- Initially uniform gas
- axisymmetric part of gravity balances with rotation at the initial state



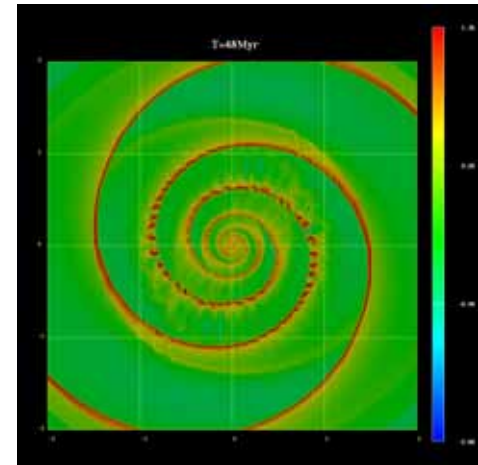
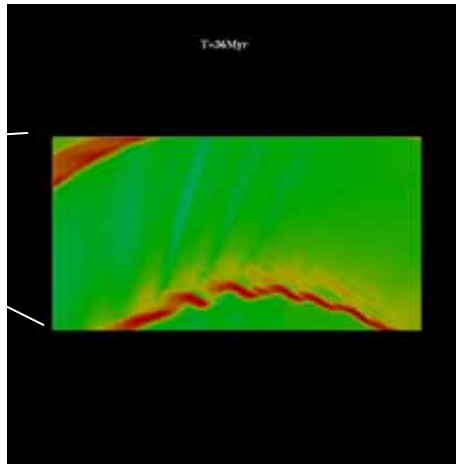
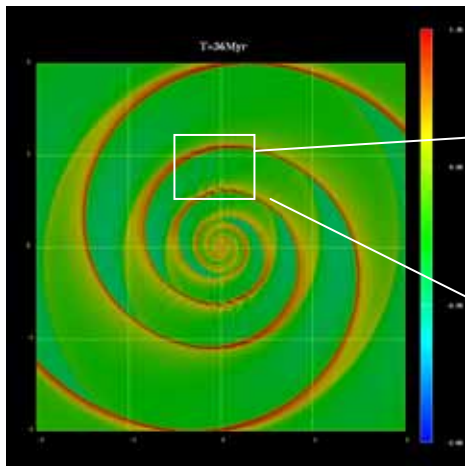


# Global MHD Simulations of the Wiggle Instability

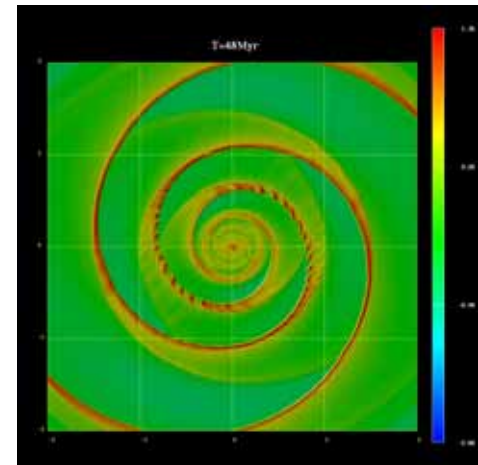
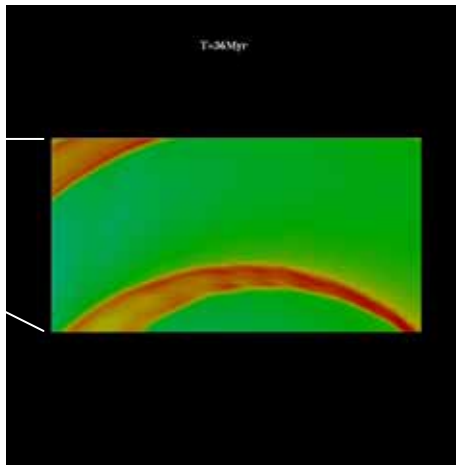
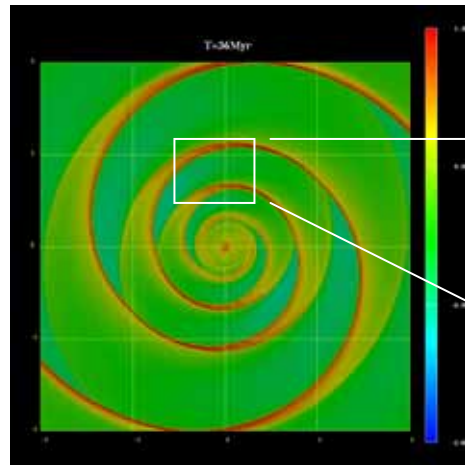
- We assume initially force free, toroidal magnetic fields:  
 $\beta = P_{\text{gas}}/P_{\text{mag}} = 10$  at  $r = 1 \text{ kpc}$
- Simulation Code : CANS
- Simulation Engine : MLW
- Simulation region :  $4 \text{ kpc} \times 4 \text{ kpc}$
- Number of Grid Points:  $2048 \times 2048$

# Numerical Results

HD  
Model



MHD  
Model

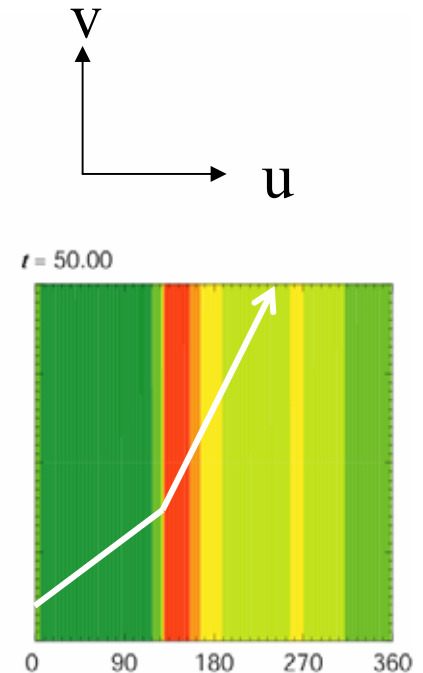
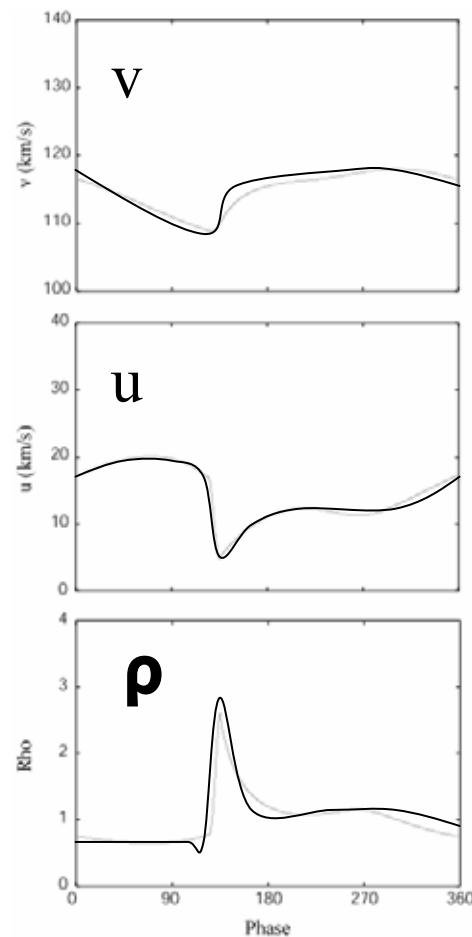
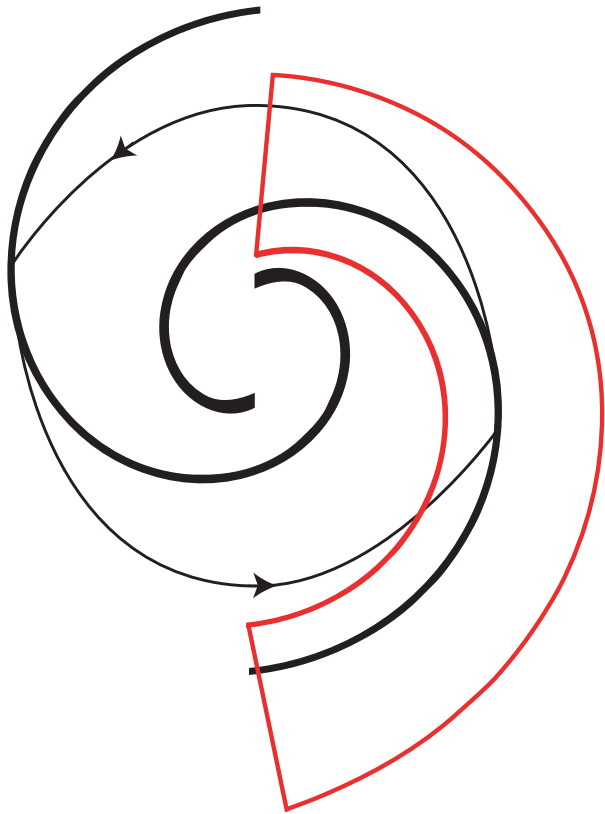


T=36 Myr

enlarged (36 Myr)

T=48 Myr

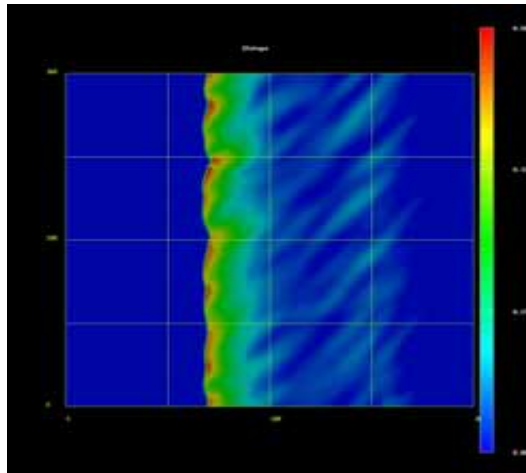
# Local Simulations of the Wobble Instability: Are Global Effects Essential ?



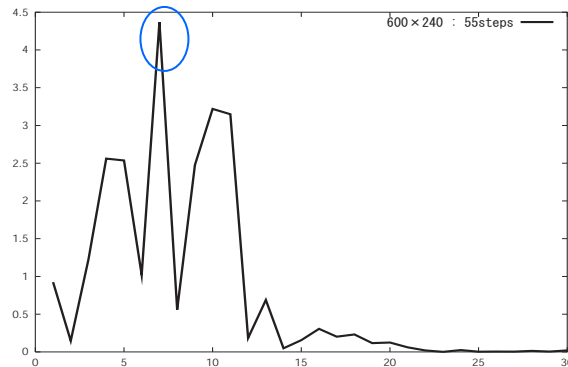
1D steady solution  
of galactic spiral  
shock (van Albada  
et al. 1982)

# Numerical Results for Hydrodynamical Model

600 × 240 mesh

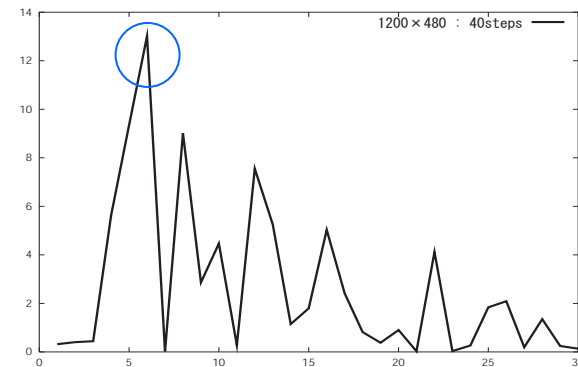
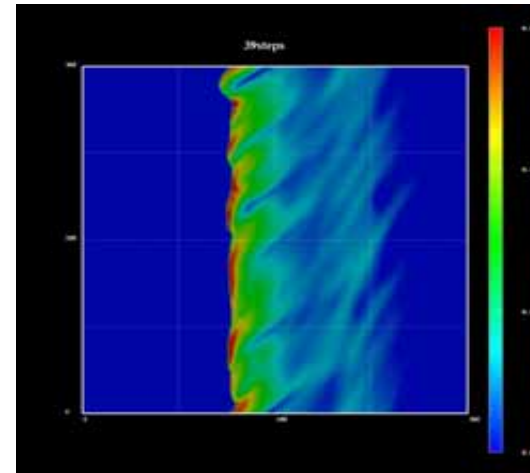


Fourier  
Amplitude



Mode number

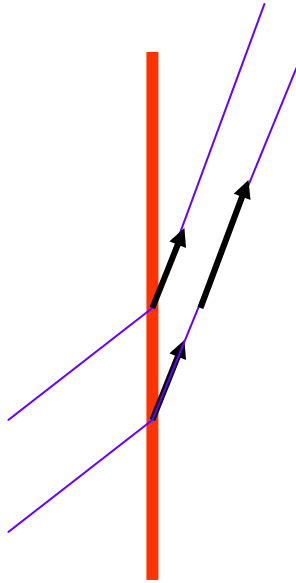
1200 × 480 mesh



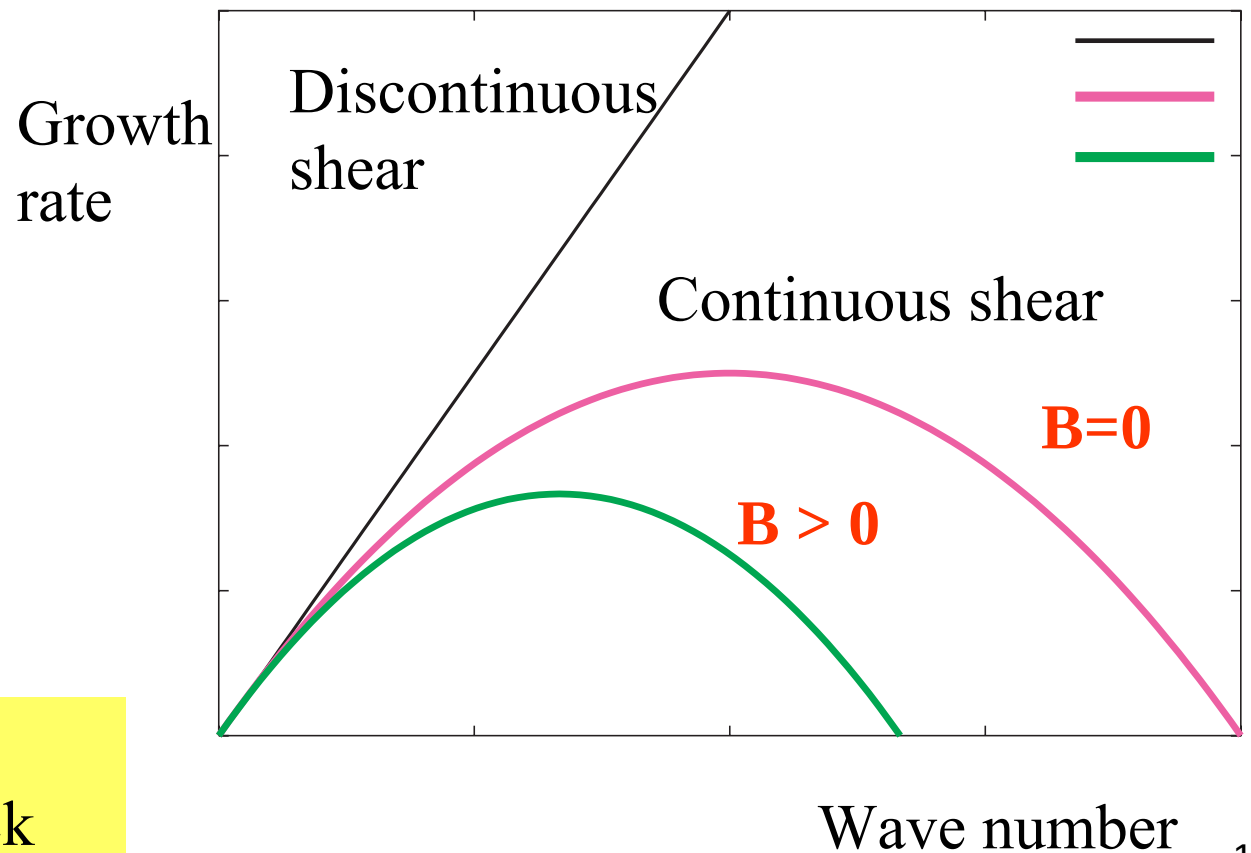
Mode number

# Mechanism of the Instability

Spiral shock



KH instability  
behind the shock

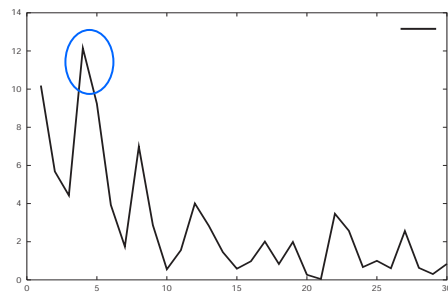
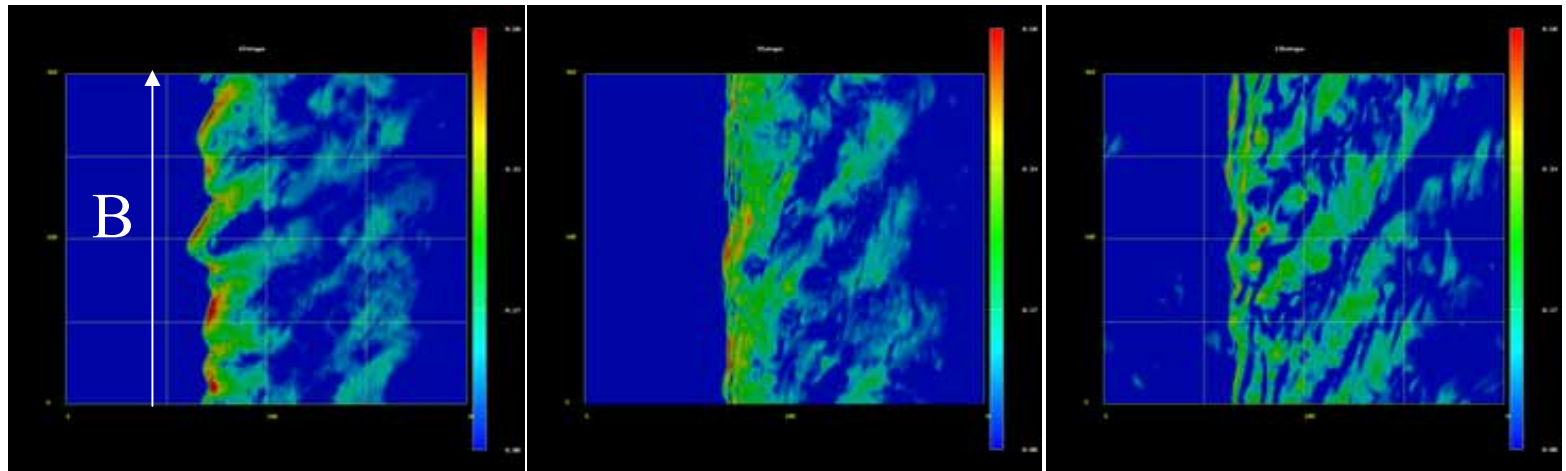


# Numerical Results for MHD Models

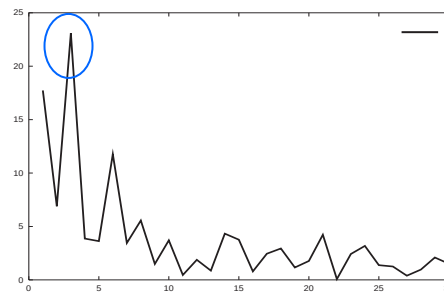
Weak field



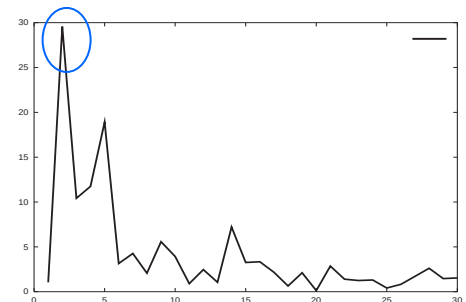
Strong field



$\beta = 1000$   
 $k=4$



$\beta = 100$   
 $k=3$



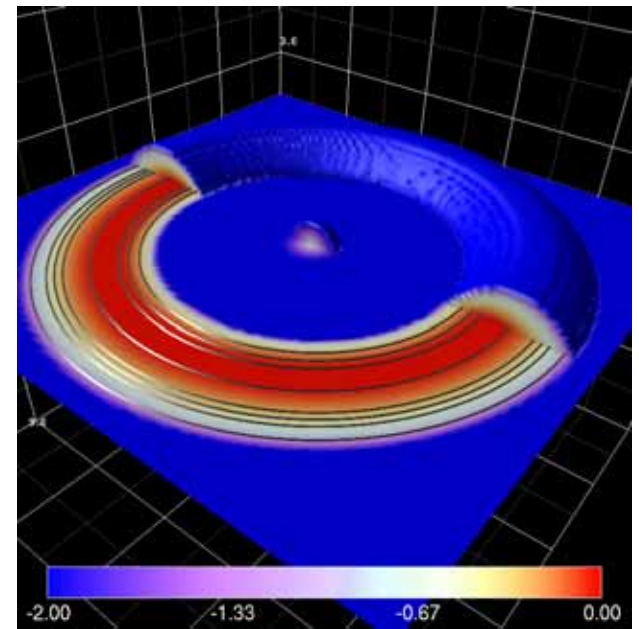
$B = 5$   
 $k=2$

$600 \times 240$   
mesh



# Global 3D MHD Simulations of Galactic Gas Disks

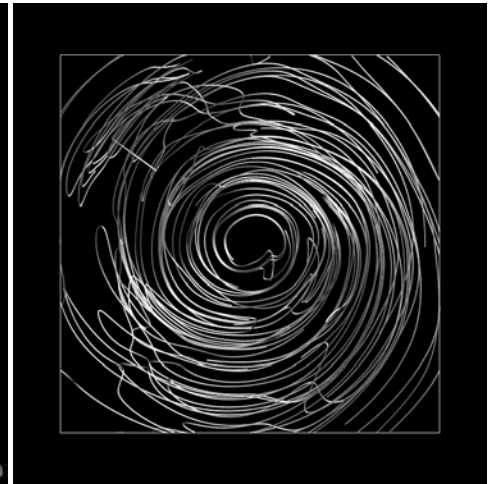
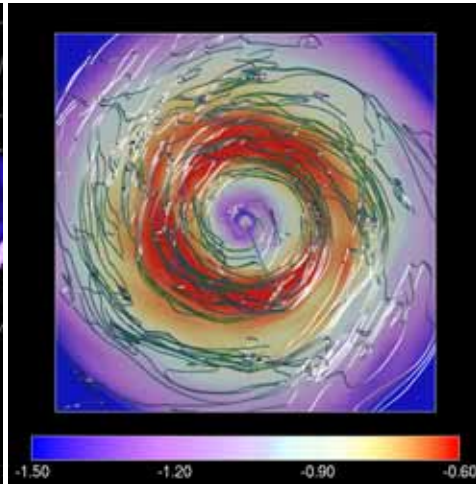
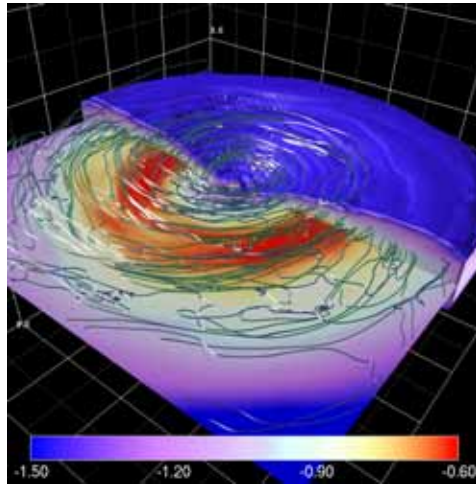
- Gravitational Potential
  - Axisymmetric potential given by Miyamoto (1980) including dark matter
- Initial state
  - Constant angular momentum torus at 10kpc
  - Weak toroidal magnetic field ( $\beta=100,1000$ )
- Anomalous resistivity
- Absorbing boundary at  $r=0.8\text{ kpc}$



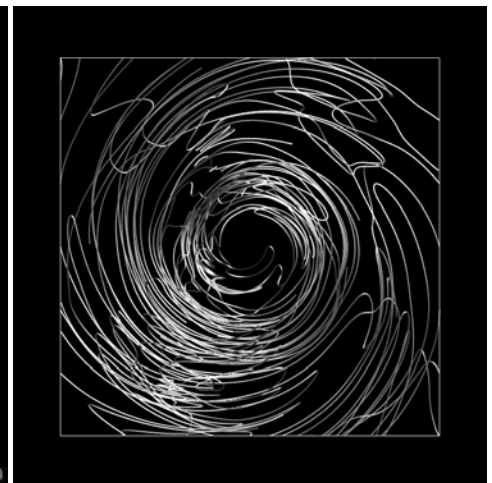
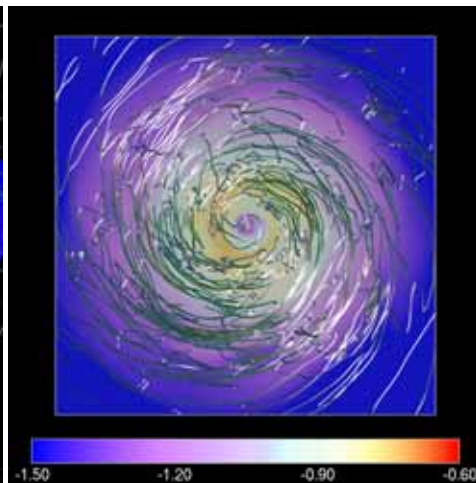
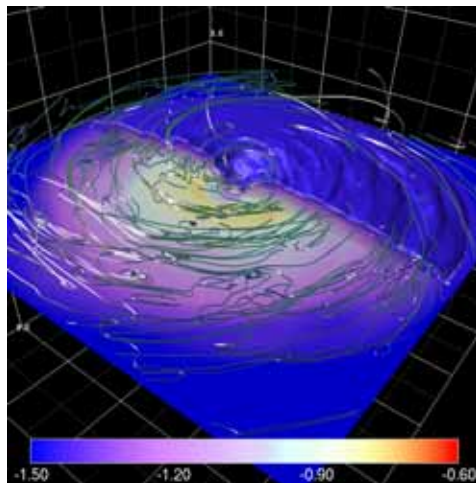
250\*64\*319 mesh

# Numerical Results ( $\beta=100$ )

2Gyr



3.5Gyr

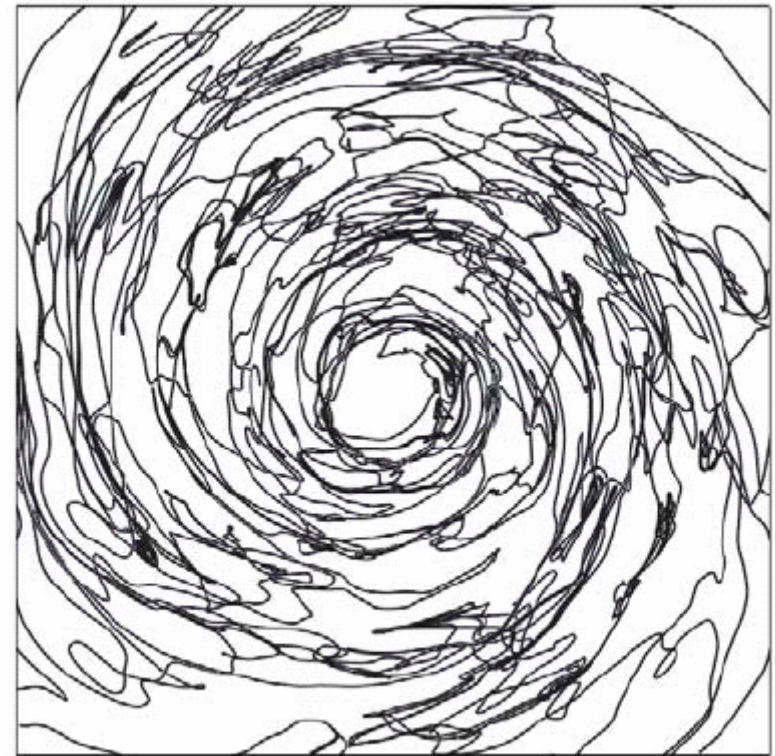
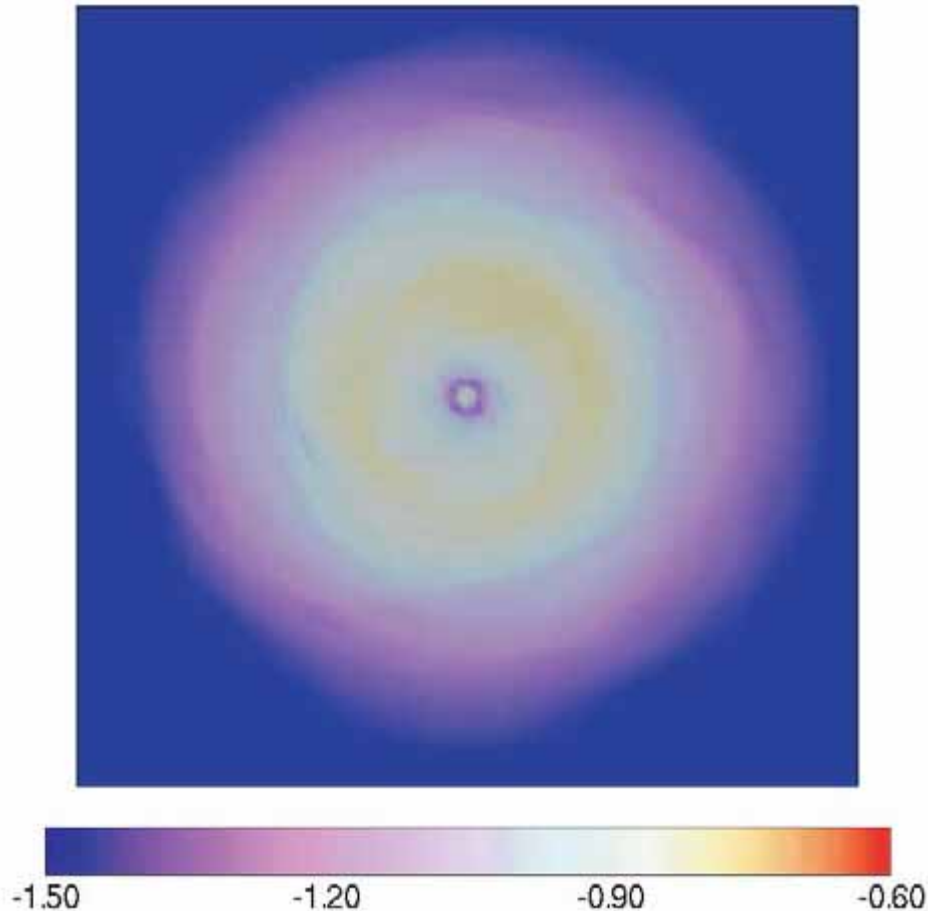


$\rho + B$

Raw field

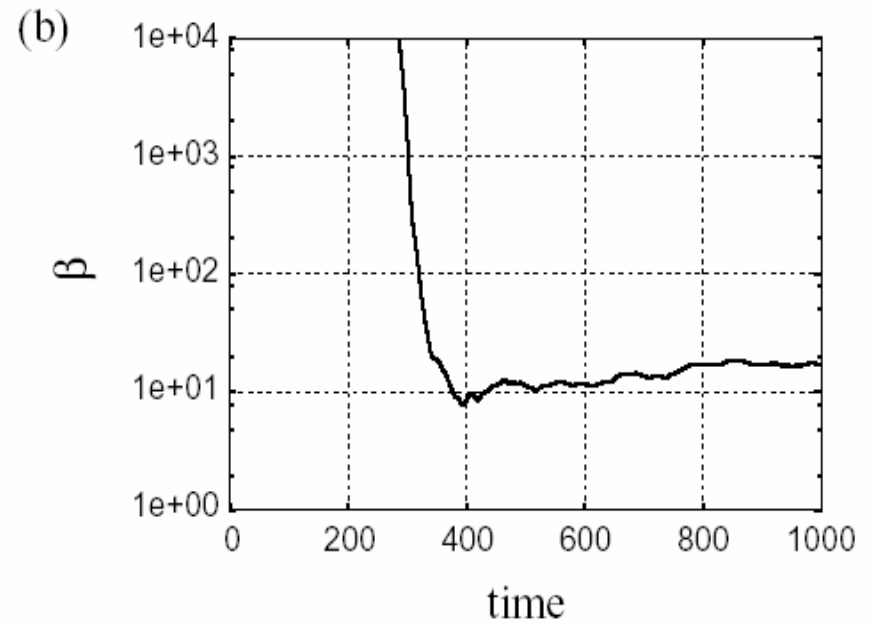
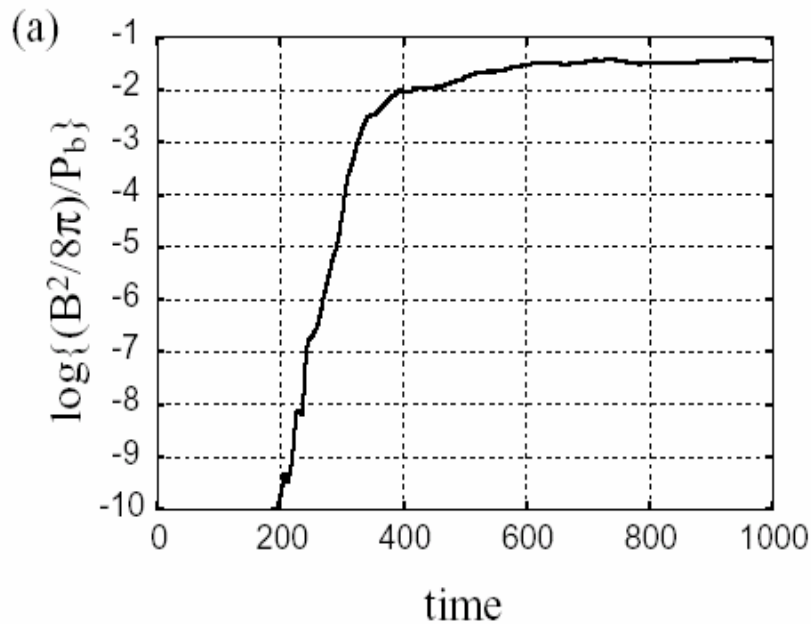
Mean field

# Density Distribution and Magnetic Field Lines



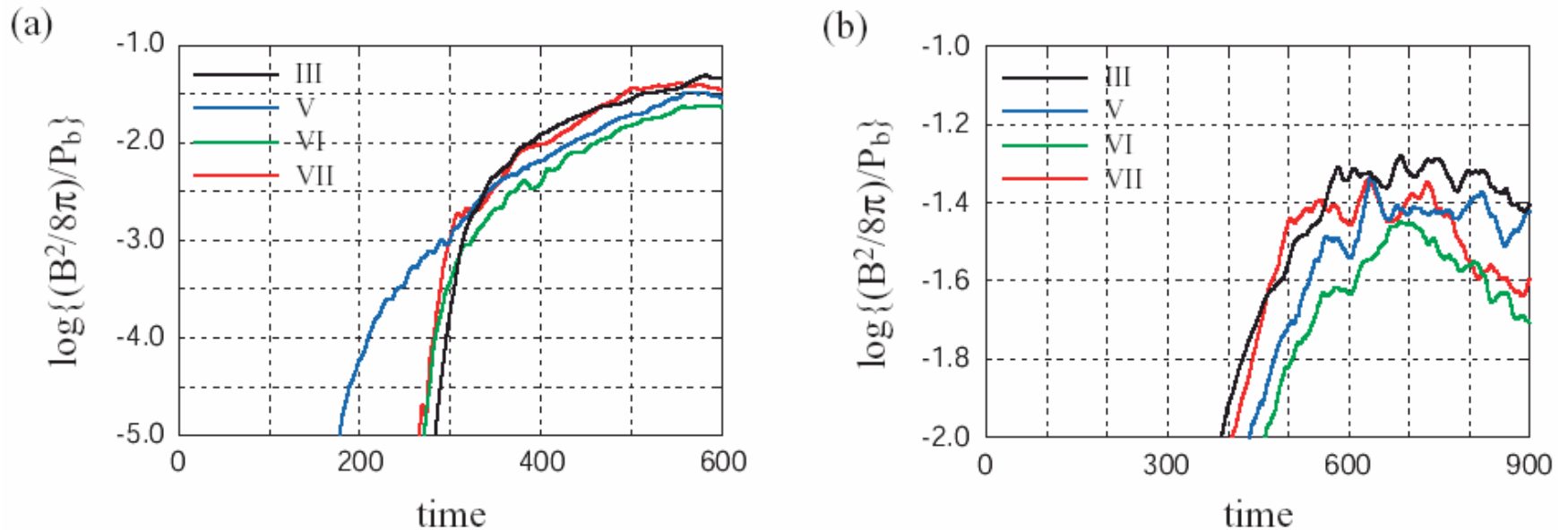
$t = 3.8\text{Gyr}$

# Growth of Magnetic Field



Average in  $2\text{kpc} < r < 5\text{kpc}$  and  $0 < z < 1\text{kpc}$

# Dependence on Azimuthal Resolution and Simulation Region



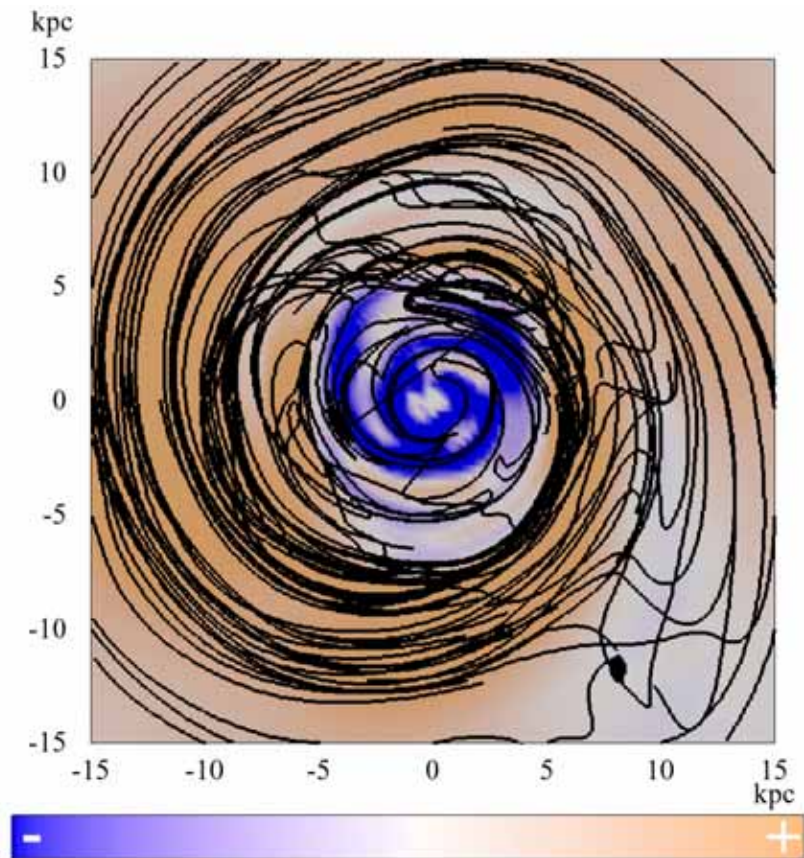
Model III: Full Circle Simulation with  $\Delta \phi = 2\pi/64$

Model V-VII:  $\frac{1}{4}$  Circle Simulation ( $0 < \phi < \pi/2$ ) with

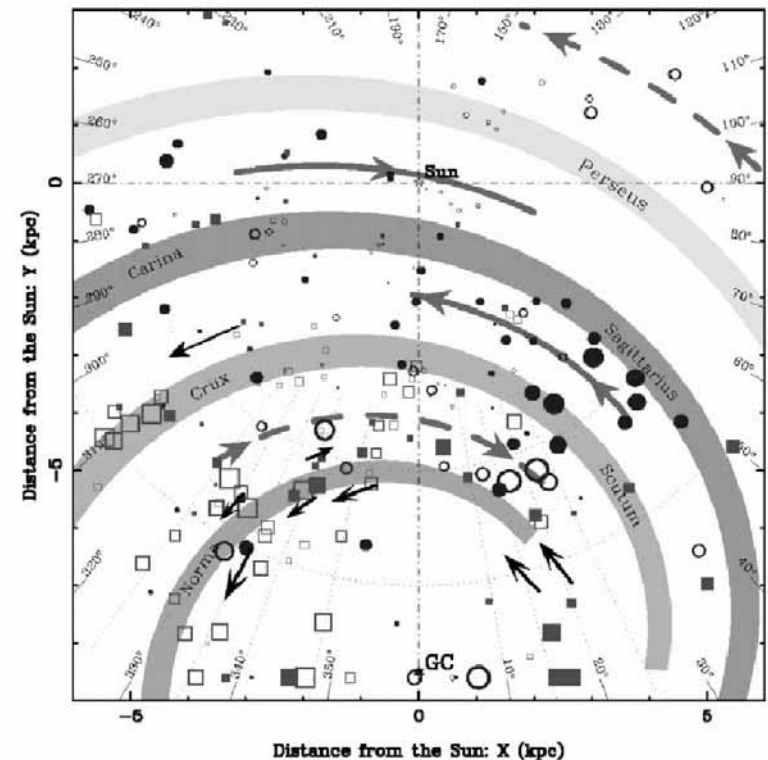
V:  $\Delta \phi = \pi/128$  VI:  $\Delta \phi = \pi/64$  VII:  $\Delta \phi = \pi/32$



# Reversal of Azimuthal Magnetic Field

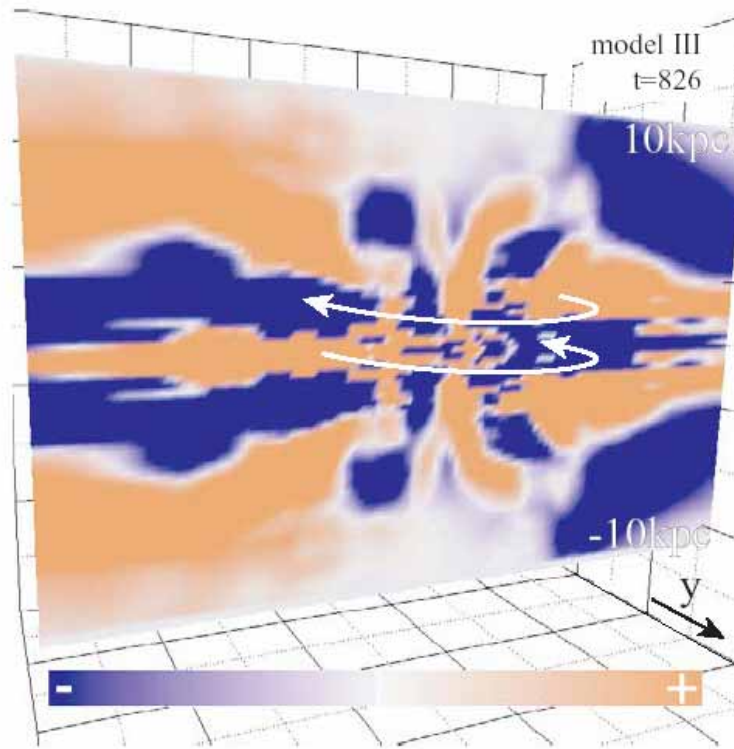


Azimuthal field at  $t=3.8$  Gyr at  $z=0.25$  Kpc

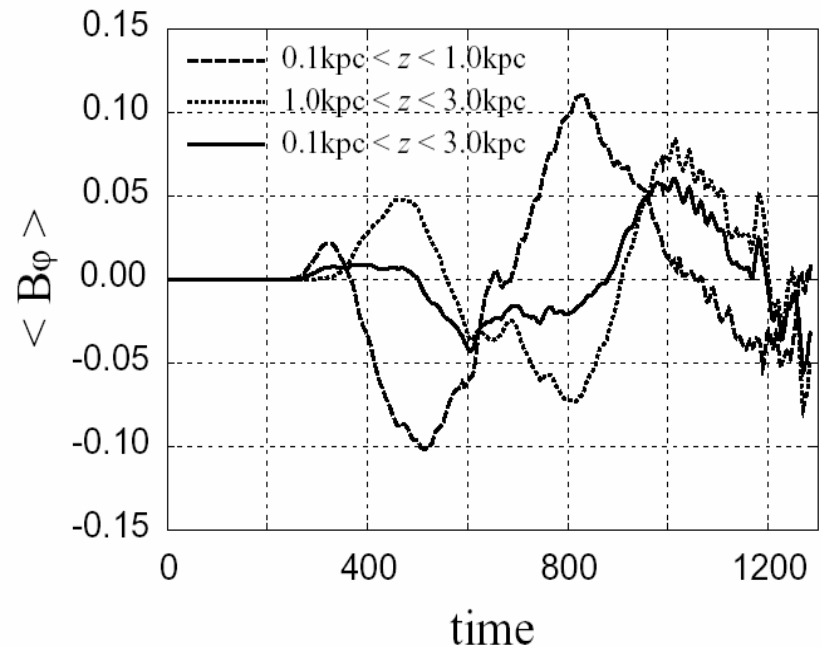


Galactic magnetic field  
obtained by Rotation Measure  
(Han et al. 2001)

# Spacial and Temporal Reversal of Azimuthal Magnetic Fields



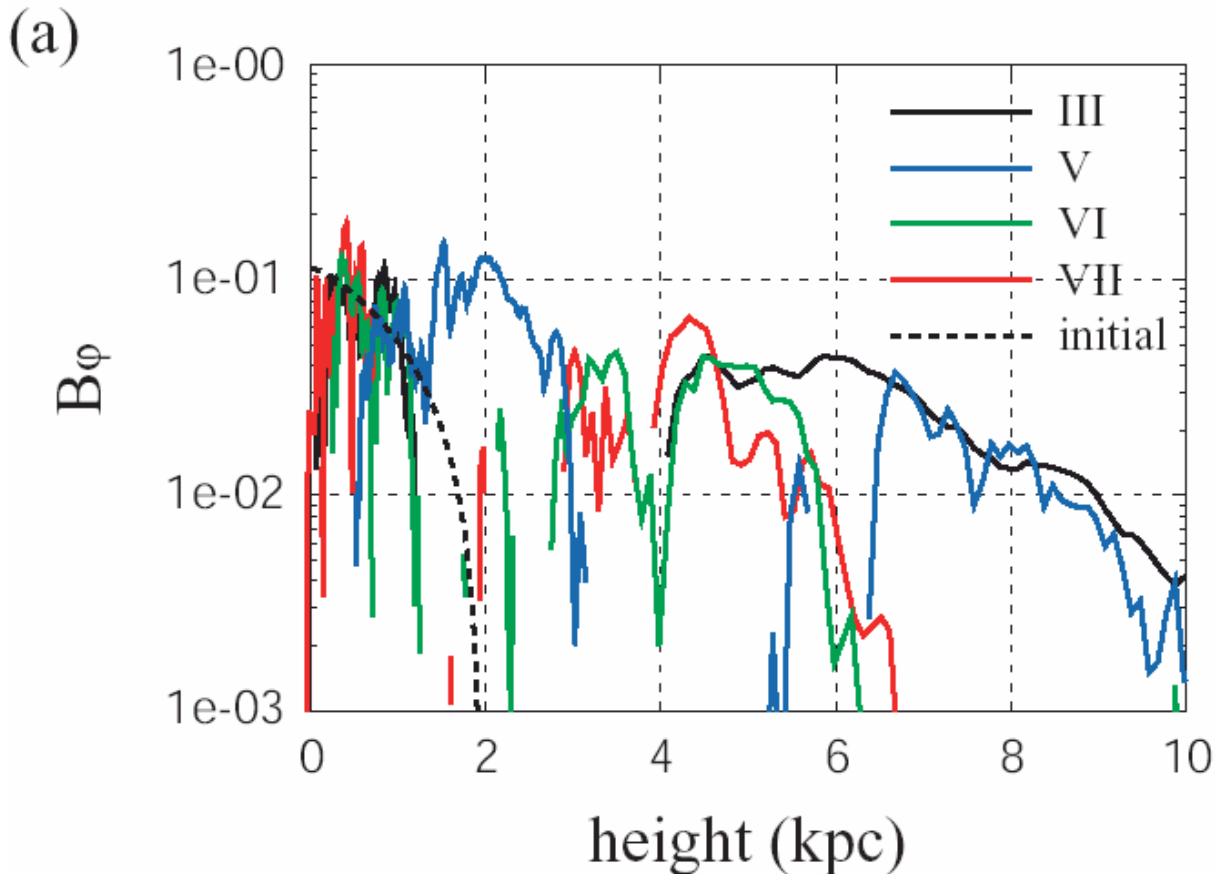
Azimuthal Magnetic Field at  $t=3.1$  Gyr



Time variation of mean azimuthal field at  $5 \text{ kpc} < r < 6 \text{ kpc}$  and  $0 < z < 1 \text{ kpc}$

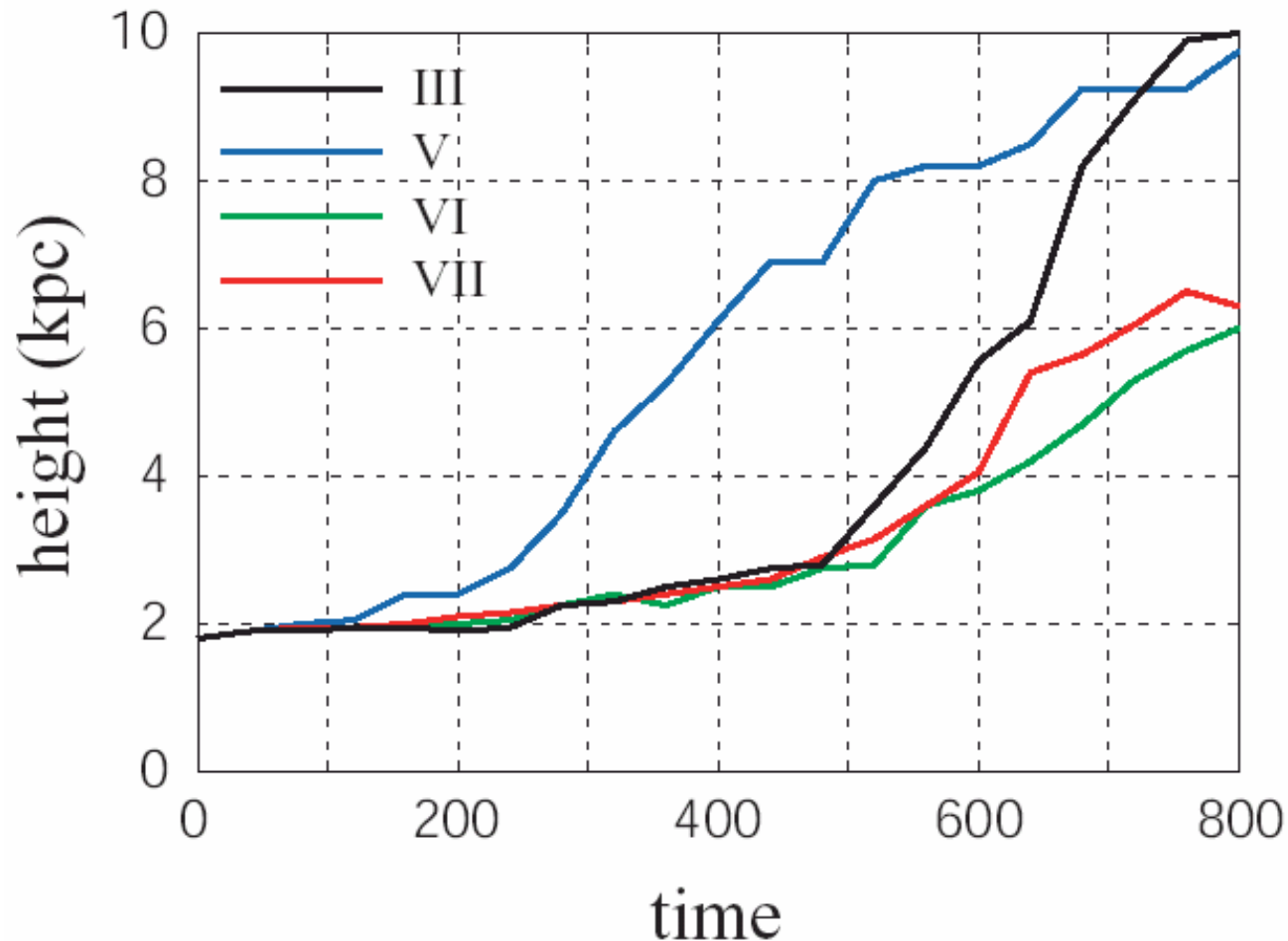


# Buoyant Rise of Azimuthal Magnetic Flux

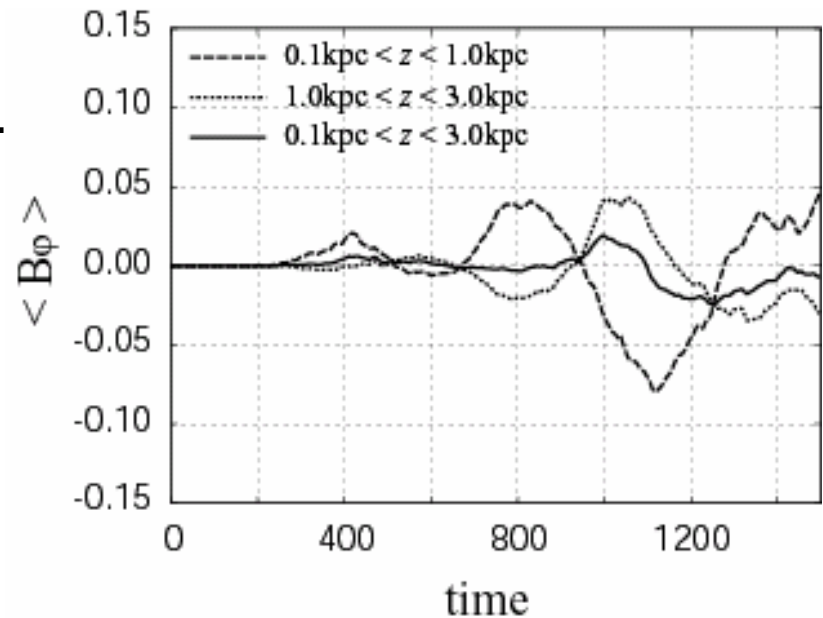
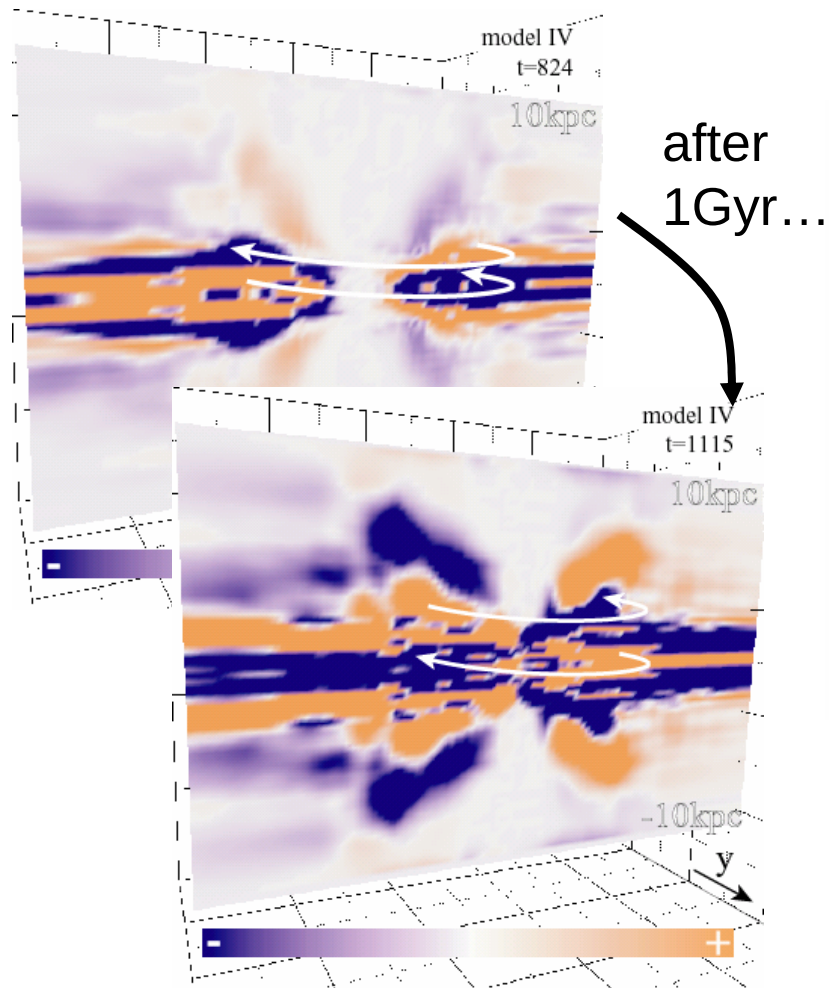


Distribution of azimuthal field at  $r=10$  kpc at  $t=3$  Gyr

# Motion of the Wavefront of Rising Magnetic Flux



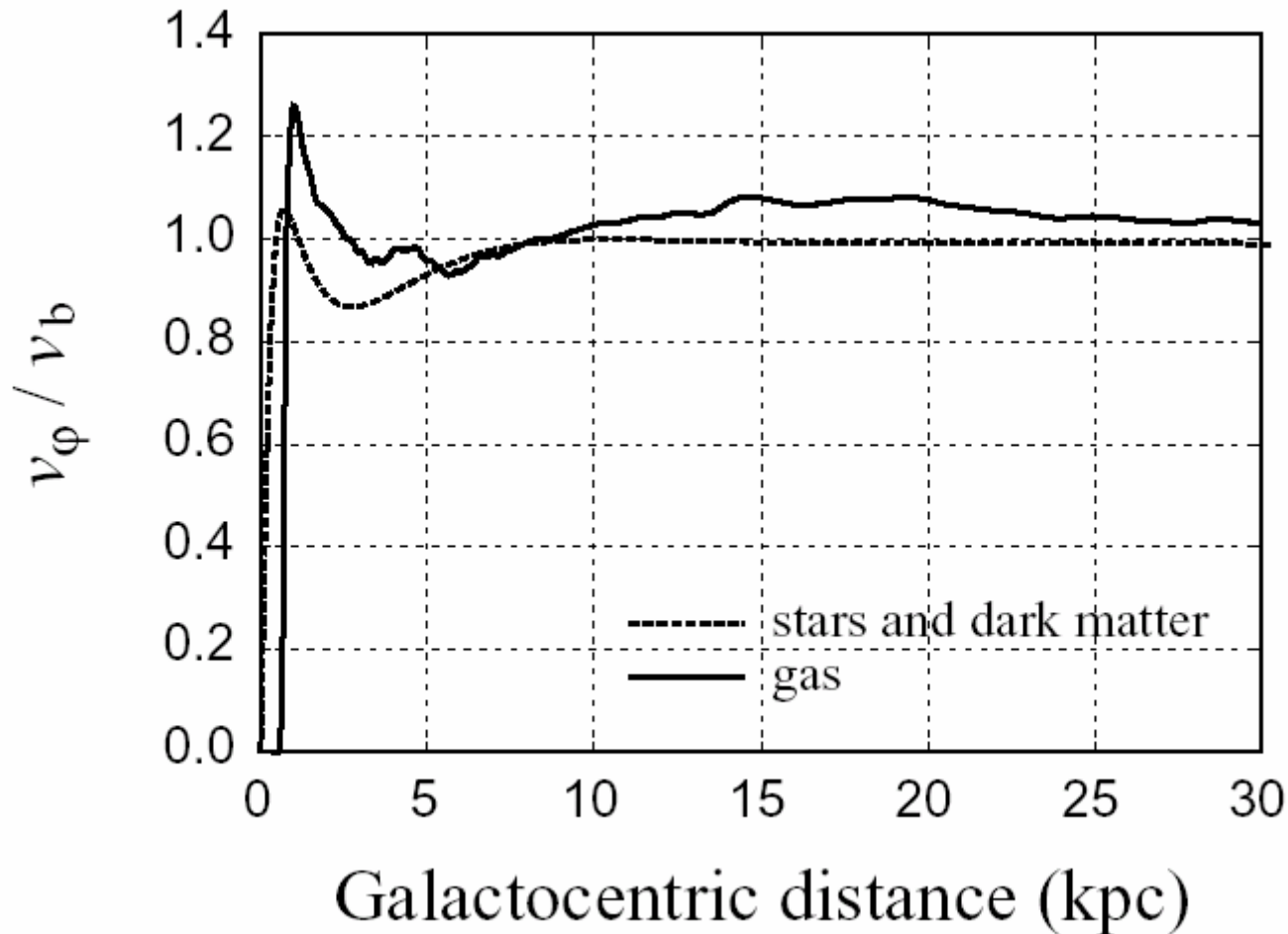
# Numerical Results for a Model with $\beta = 1000$



Time variation of mean azimuthal magnetic field

At  $5\text{kpc} < r < 6\text{kpc}$

# Rotation Curves for Stars/Dark matter and Gas



# Discussion

- Magnetic field strength
  - Amplification of magnetic field saturates when  $\beta \sim 10$ . The final field strength ( $\sim \mu\text{G}$ ) is smaller than the Galactic magnetic field
  - Non-axisymmetric gravitational potential, Supernova explosions, and/or cooling of the interstellar gas may further amplify magnetic fields
- Infall of the interstellar gas
  - Interstellar gas loses angular momentum by Maxwell stress and infalls with accretion rate  $0.001 M_{\text{sun}}/\text{yr}$  when the initial torus has  $5 \cdot 10^8 M_{\text{sun}}$

# Summary

- We studied the stability of the galactic spiral shock and showed by local and global simulations that even when the magnetic fields are included, wiggle instability grows.
- 3D global MHD simulations of the galactic gas disks under axisymmetric gravitational potential showed that  $\mu$  G magnetic fields are maintained
- The direction of azimuthal magnetic fields reverses both in space and time.
- Other mechanisms such as non-axisymmetric gravitational potential and/or supernova explosions may further amplify magnetic fields.