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【MHD2017】 磁気流体プラズマで探る高エネルギー天体現象研究会 August 28, 2017 (東京)

### Since I moved to Osaka, ...

- MHD Simulation + Laser Experiment
- Keywords: Plasma Physics, Magnetic Field
- Target: Boundary between Laboratory (Laser) Plasma and Astrophysical Plasma
  - MHD Turbulence (MRI, Dynamo)
  - High-Pressure Physics (HEOS) Jupiter, ICF
  - Interfacial Instability (RMI, RTI) ISM, ICF
  - Particle Acceleration (PIC) LPI + B





## To understand the saturation of MRI is an ultimate goal of accretion disk study.

- What is the origin of "alpha"?
  - Local Shearing Box
  - Non-ideal MHD Effects (Ohmic & Hall)
  - Pressure Dependence?
- What determines the saturation?
  - Magnetic Field Geometry
  - Dissipation
  - Magnetic Prandtl Number
  - Global Effect (Wind)
  - Convection?

## MRI turbulence is the most promising mechanism of angular momentum transport.

- Origin of Turbulence in Accretion Disks
- Key Ingredients
  - (Weak) Seed Field
  - Differential Rotation





- Field Amplification (Dynamo)
- Different Rotation in the Sun → Unstable?

### Convection zone in the Sun could be unstable for MRI.

- Higher Latitude Tachocline
- Near Surface Shear Layer (NSSL)



Linear stability for MRI is examined with a radial shear in the vertical velocity.

#### **Unperturbed State**

- Uniform Density & Pressure
- Differential Rotation & Vertical Shear Flow  $v_0 = (0, -q\Omega x, v_{z0}(x))$   $\Lambda^{\Omega}$
- Sinusoidal Shear

$$v_{z0} = v_0 \cos(k_0 x)$$

Uniform Vertical Magnetic Field



 $\boldsymbol{B}_0 = (0, 0, B_0)$ Two Major Parameters of This Analysis

$$K_0 = \frac{v_{A0}k_z}{\Omega} \quad \& \quad V_0 = \frac{v_0}{v_{A0}}$$

#### The growth rate is given by complex eigenvalues of 2nd order dispersion equations.

$$D\left(\frac{\delta P}{\rho_0} + v_{A0}^2 \frac{\delta B_z}{B_0}\right) = \frac{\left(\sigma^2 - v_{A0}^2 k_z^2\right)^2 - \kappa^2 \left(\sigma^2 - v_{A0}^2 k_z^2\right) - 4\Omega^2 v_{A0}^2 k_z^2}{\sigma \left(\sigma^2 - v_{A0}^2 k_z^2\right)} \left(i\delta v_x\right)$$

$$D(i\delta v_x) = -(Dv_{z0})\frac{k_z}{\sigma}(i\delta v_x) + \frac{\sigma k_z^2}{\sigma^2 - v_{A0}^2 k_z^2} \left(\frac{\delta P}{\rho_0} + v_{A0}^2 \frac{\delta B_z}{B_0}\right)$$
$$\sigma \equiv \omega - v_{z0}k_z \qquad v_{A0}^2 \equiv \frac{B_0^2}{4\pi\rho_0}$$

Periodic Boundary Condition

 $i\delta v_x = 0$  or  $D(i\delta v_x) = 0$  at  $k_0 x = \pm \pi$ 

- Searched in Complex Space

### KHI in the shearing box is suppressed by differential rotation.



### If the shear velocity exceeds the Alfven speed, the growth of MRI is reduced significantly.

- Reduction of MRI Growth
- Appearance of KHI Mode



### Linear growth of MRI is killed or regulated by convection (turbulent) motion.

#### Conditions:

- Shear wavelength is comparable to  $v_{A0}/\Omega$
- Shear velocity is 10 times faster than Alfven speed.



### Interfacial Magneto-Hydrodynamic Instabilities in Laser Plasmas

### Collaborators

#### Simulation & Theory

- K. Nishihara (Osaka U)
- C. Matsuoka (Osaka City U)
- T. Inoue (Nagoya U)
- J. G. Wouchuk (UCLM, Spain)

#### Laser Experiment



- Y. Sakawa, S. Fujioka, K. Shigemori, S. Tamatani, M. Murakami,
  R. Kumar, K. Matsuo (Osaka U)
- T. Morita (Kyushu U)
- M. Koenig, B. Albertazzi, T. Michel, G. Rigon (LULI, France)
- A. Casner (CEA, France)



### Laser Experiment



#### GEKKO XII Laser at ILE, Osaka U Laser Wavelength: 0.35 [um], Laser Energy: 1 [kJ] Pulse Duration: 2.5 [ns], Spot Diameter: 600 [um]

### Outline

- Backgrounds
  - Why RMI? Why Magnetic Field?
- MHD RMI
- Effects of Magnetic Field
  - 1. Suppression of RMI (Theory)
  - 2. Field Amplification (Theory/Experiment)
  - 3. Anisotropic Thermal Conduction (Experiment)
- Summary





### Backgrounds

RMI-driven turbulence plays an important role in various plasma phenomena.

**Astrophysical Plasmas** 

- Supernova Shocks + Inhomogeneous Interstellar Medium
  - Origin of IS Turbulence
  - Magnetic Field Amplification

Laboratory Plasmas

- Implosion in Laser Fusion Plasma
  - "Mixing" by RMI & RTI
  - External Magnetic Field
- RMI + Magnetic Field = ???

Supernova Remnant





Clark+ 2016

### Generation of kilo-Tesla magnetic fields has been achieved by high-power lasers.

- Strong B Field Available in Laser Exp.
- Method (Using GEKKO Laser in Osaka)
  - Coil + Compression
  - Capacitor Coil

cf.) 1kT = 10MG, Permanent Magnet  $\sim$ 1T



Korneev + 2015

#### Laser experiments can treat RMI in highenergy-density plasmas.

"Low Energy Density" RMI



Chapmann & Jacobs 2006

#### Laser experiments can treat RMI in highenergy-density plasmas.

- "Low Energy Density" RMI
- "High Energy Density" RMI
  - High Mach Number Shock
  - Plasma Flow
  - Magnetic Field 年
- Laser Plasma RMI
  - Ablative RM-type Instability
  - Classical RMI (Heavy-to-Light)



**Experimental Result** 

Chapmann & Jacobs 2006



### The key ingredients of RMI is a shock wave and corrugated contact discontinuity.



### Driving engine of RMI is the vorticity deposited at the corrugated interface.

• Mechanism: Tangential Flows Caused by Refraction Motion at Oblique Shock Surface



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 Mechanism: Tangential Flows Caused by Refraction Motion at Oblique Shock Surface

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Growth Velocity



Wouchuk & Nishihara 1996; 1997

#### **Characteristics of RMI**

- Linear Growth with Time
- Without Gravity
- Unstable for Both <u>Light-</u> <u>to-Heavy</u> & <u>Heavy-to-</u> <u>Light</u> Configurations



### There are some formula predicting the linear growth velocity of RMI theoretically.

Asymptotic Growth Velocity Wouchuk & Nishihara 1997



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• Asymptotic Growth Velocity Wouchuk & Nishihara 1997



Important effects of B fields on RMI have shown by simulations and experiments.

- 1.Suppression of RMI Growth by a Strong Magnetic Field
- 2.Amplification of a Magnetic Field by RMI Turbulent Motions

3.Energy Confinement Due to Anisotropic Thermal Conduction

### 1. Suppression of RMI

#### **MHD Simulations**

Samtaney 2003 Wheatley et al. 2005; 2009 Sano+ PRL 2013

## Basic equations for numerical RMI simulations<sup>™</sup> are standard ideal MHD equations.

Ideal MHD Equations

$$\begin{aligned} \frac{\partial \rho}{\partial t} + \boldsymbol{\nabla} \cdot (\rho \boldsymbol{v}) &= 0 \\ \frac{\partial \rho \boldsymbol{v}}{\partial t} + \boldsymbol{\nabla} \cdot \left[ \left( P + \frac{B^2}{8\pi} \right) \boldsymbol{I} + \rho \boldsymbol{v} \boldsymbol{v} - \frac{\boldsymbol{B} \boldsymbol{B}}{4\pi} \right] &= 0 \\ \frac{\partial e}{\partial t} + \boldsymbol{\nabla} \cdot \left[ \left( e + P + \frac{B^2}{8\pi} \right) \boldsymbol{v} - \frac{(\boldsymbol{B} \cdot \boldsymbol{v}) \boldsymbol{B}}{4\pi} \right] &= 0 \\ \frac{\partial \boldsymbol{B}}{\partial t} &= \boldsymbol{\nabla} \times (\boldsymbol{v} \times \boldsymbol{B}) \qquad \qquad e = \frac{P}{\gamma - 1} + \frac{\rho v^2}{2} + \frac{B^2}{8\pi} \end{aligned}$$

- Numerical MHD Scheme
  - Godunov-type Grid-base Scheme with an Approximate MHD Riemann Solver (Sano+ ApJ 1998)
  - CMoC-CT for the Field Evoluton (Clarke 1996)

## Initial setup for the single-mode analysis is characterized by only 4 parameters.

- 2D Initial Configuration
- 4 Non-Dimensional Parameters
- 1. Mach Number

 $M = |U_i|/c_{s1}$ 

2. Density Jump



3. Corrugation Amplitude  $\psi_0/\lambda$ 

4. Field Strength  $\beta_0 = 8\pi P_0/B_0^2$ 



SIM

# RMI growth can be reduced if a magnetic field is larger than a critical value.

Plasma beta gives the criteria?



# RMI growth can be reduced if a magnetic field is larger than a critical value.

0.5

12

10

8

6

4

 $\rho/\rho_1$ 

(c)

- Plasma beta gives the criteria?
- No, not so simple...
- Critical strength depends on the Mach number of incident shock.



# RMI growth can be reduced if a magnetic field is larger than a critical value.

- Plasma beta gives the criteria<sup>(\*)</sup>
- No, not so simple...
- Critical strength depends on the Mach number of incident shock.
- Key Process: <u>Extraction</u> of the Vorticity from the <u>Interface</u>

Samtaney 2003 Wheatley et al. 2005; 2009



## For HD cases, the vorticity deposited at the I interface stays there and drives RMI.



During the growth of the RMI, vorticity is always associated with the CD.
When B fields exist, the vorticity travels  $awa_y^{SM}$  from the interface by Alfven wave.

 Vortex sheet is moving away from the contact surface!
 Sano+ PRL 2013



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 Vortex sheet is moving away from the contact surface!
 Sano+ PRL 2013



#### Critical stability condition is determined by the Alfven (Mach) number for RMI.

SIM

Alfven Number for RMI

$$R_A \equiv rac{v_{
m lin}}{v_A^*}$$
 — WN Formula

#### Critical stability condition is determined by the Alfven (Mach) number for RMI.

Alfven Number for RMI

$$R_A\equiv rac{v_{
m lin}}{v_A^*}$$
  $\leftarrow$  WN Formula

- Critical Value ~ 10
  - Independent of Mach Number, 0.1
     Density Ratio, Perturbation Amplitude, and Field Direction!

$$(\rho_2/\rho_1, \psi_0/\lambda) = (0.1, 0.1) \& B_y = (0.5, 0.1) \& B_y = (0.1, 0.03) \& B_y = (0.1, 0.1) \& B_x = (10, 0.1) \& B_y$$

**Field** Suppressed Х  $\overline{\mathbf{\cdot}}$ 0  $\bigcirc$ 0.01 $\bigcirc$ **Unstable** 10 100 M

SIM

Stronger

#### Critical stability condition is determined by the Alfven (Mach) number for RMI.

Alfven Number for RMI

$$R_A\equiv rac{v_{
m lin}}{v_A^*}$$
 and the second seco

- Critical Value ~ 10
  - Independent of Mach Number, 0.1
     Density Ratio, Perturbation Amplitude, and Field Direction!
- Consistent with
   <u>Current-Vortex Sheet</u>
   <u>Model</u> Matsuoka+ JNS 2017



SIM

#### Critical field strength for the suppression in laser plasma is estimated as about 10T.

- This will be tested experimentally soon.
- For Stability (Laser Exp. Condition)  $R_A < 10$  $B > B_c \approx 0.1 \times (4\pi \rho^*)^{1/2} v_{\text{lin}}$

SIM



# 2-1. Amplification of a Magnetic field

MHD Simulations & Current-Vortex Sheet Model Sano+ ApJ 2012 Matsuoka+ JNS 2017

#### Ambient magnetic fields can be amplified dramatically by RMI motions.

SIM



#### Ambient magnetic fields can be amplified dramatically by RMI motions.



SIM

#### Growth rate of B field agrees fairly well with <sup>SM</sup> the stretching rate of interface.

• Amplification by Stretching Term in Induction Eq.



### Field amplification process is independent of <sup>™</sup> the initial field direction.

• Saturation level is independent of any parameters; Mach number, density jump, & fluctuation amplitude.



Saturation level of field strength is of the order of turbulent kinetic energy.

• The maximum field strength is limited by the growth (turbulent) velocity of RMI.

SIM



#### Saturation level of field strength is of the order of turbulent kinetic energy.

• The maximum field strength is limited by the growth (turbulent) velocity of RMI.

SIM

![](_page_48_Figure_2.jpeg)

## Magnetic field amplification occurs also in 3D<sup>™</sup> RMI, and the amplitude is slightly larger.

![](_page_49_Picture_1.jpeg)

Initial Modulation Function  $\psi_{\rm 3D} = \psi_0 \cos(ky) \cos(kz)$ 

## Magnetic field amplification occurs also in $3D^{SM}$ RMI, and the amplitude is slightly larger.

![](_page_50_Picture_1.jpeg)

![](_page_50_Picture_2.jpeg)

![](_page_50_Figure_3.jpeg)

![](_page_50_Picture_4.jpeg)

### Complicated "filamentary" field structures are formed in multi-mode fluctuation cases.

![](_page_51_Figure_1.jpeg)

#### Filamentary structures in RMI remind us interstellar turbulence driven by SN shocks.

Supernova Shock + Density Fluctuation in ISM

SIM

 RMI turbulence shows many similarities to Interstellar turbulence.

![](_page_52_Figure_3.jpeg)

# 2-2. Amplification of a Magnetic field

Experimental Results by GEKKO Laser in Osaka

Preliminary

#### Classical RMI experiment using high-power lasers have been carried out by many groups.

- NOVA Laser
  - Be/Foam, Be/CH
    Dimonte & Remington 1993
    Farley+ 1996
- OMEGA Laser
  - CHBr/FoamGlendinning+ 2003
- Nike Laser
  - Foam/CH e.g., Aglitskiy+ 2006
- X-ray Diagnostics

![](_page_54_Figure_8.jpeg)

#### Glendinning+2003

### Classical RMI experiment using high-power lasers have been carried out by many groups.

- NOVA Laser
  - Be/Foam, Be/CH
    Dimonte & Remington 1993
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- OMEGA Laser
  - CHBr/Foam Glendinning+ 2003
- Nike Laser
  - Foam/CH e.g., Aglitskiy+ 2006
- X-ray Diagnostics

- GEKKO Laser at Osaka
  - CH/N2 Gas
  - Inclusion of B Field
  - Optical Measurement

![](_page_55_Figure_13.jpeg)

Koenig+ PoP 2017

#### Laser experiment on self-generated field is $^{\text{EXP}}$ one of the hot topics in "laser astrophysics".

- 1. Generation of B Field
  - Biermann Battery Process
- 2. Field Amplification
  - Amplification of Self-Generated Field by Turbulence Driven by Shock + "Mesh" Top view

 $-\nabla n_e \times \nabla p_e / e n_e^2$ 

![](_page_56_Figure_5.jpeg)

#### Laser experiment on self-generated field is $^{\text{EXP}}$ one of the hot topics in "laser astrophysics".

- 1. Generation of B Field
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- 2. Field Amplification
  - Amplification of Self-Generated Field by Turbulence
     Driven by Shock + "Mesh"

 $-\nabla n_e \times \nabla p_e / e n_e^2$ 

 Amplification of an External Seed Field by Turbulence Driven by RMI

![](_page_57_Figure_6.jpeg)

#### Why laser experiment? --- It is because of magnetized plasma and high Mach number.

- Initial Interface
  - Modulated CH Foil (50 umt)
    - Wavelength: 150 um
    - Amplitude: 7.5 um
  - Nitrogen Gas
    - Pressure: 5 Torr

![](_page_58_Picture_7.jpeg)

![](_page_58_Figure_8.jpeg)

Experimental Setup

EXP

![](_page_59_Picture_0.jpeg)

2016 FM02

![](_page_60_Picture_0.jpeg)

![](_page_60_Picture_1.jpeg)

2016 FM02

#### Why laser experiment? --- It is because of magnetized plasma and high Mach number.

- Initial Interface
  - Modulated CH Foil (50 umt)
    - Wavelength: 150 um
    - Amplitude: 7.5 um
  - Nitrogen Gas
    - Pressure: 5 Torr
- Magnetic Field
  - Neodymium Magnet
    - Strength: 0.2 T

![](_page_61_Figure_10.jpeg)

Experimental Setup

**EXP** 

#### Why laser experiment? --- It is because of magnetized plasma and high Mach number.

- Initial Interface
  - Modulated CH Foil (50 umt)
    - Wavelength: 150 um
    - Amplitude: 7.5 um
  - Nitrogen Gas
    - Pressure: 5 Torr
- Magnetic Field
  - Neodymium Magnet
    - Strength: 0.2 T
- Laser-Driven Shock
  - GEKKO Laser
    - Energy: 0.2-0.7 kJ
    - Pulse: 2.5 ns

• Experimental Setup

**EXP** 

![](_page_62_Figure_15.jpeg)

#### Both of the transmitted shock and interface |EXP| velocities depend on the laser intensity.

![](_page_63_Figure_1.jpeg)

#### Evolution of RMI growth observed successfully by optical measurements.

**EXP** 

 Snapshot Taken by Optical Shadowgraphy

![](_page_64_Picture_2.jpeg)

#### Evolution of RMI growth observed successfully by optical measurements.

**EXP** 

 Snapshot Taken by Optical Shadowgraphy

![](_page_65_Picture_2.jpeg)

#### Evolution of RMI growth observed successfully by optical measurements.

 Snapshot Taken by Optical Shadowgraphy

![](_page_66_Picture_2.jpeg)

 Phase reversal at the very beginning was observed in the past GEKKO experiment.

![](_page_66_Figure_4.jpeg)

**EXP** 

![](_page_66_Figure_5.jpeg)

0.5

Time (ns)

1.0

1.5

-10

0.0

### Growth velocity of the surface fluctuation $can^{EXP}$ be evaluated from snapshots of the "fingers".

![](_page_67_Figure_1.jpeg)

#### Measured growth velocities are comparable or larger than the model prediction.

- Wouchuk-Nishihara Formula
  - With a Help of the **Interface Velocity** from an Empirical Fit

$$rac{v_{ ext{lin}}}{k\psi_{0}v_{i}}pprox -0.16 \, {egin{array}{c} rac{
ho_{2}}{
ho_{1}} = 10^{-5}} \ M_{i} = 5 \ \end{array}$$

![](_page_68_Figure_4.jpeg)

#### Measured growth velocities are comparable or larger than the model prediction.

- Wouchuk-Nishihara Formula
  - With a Help of the Interface Velocity from an Empirical Fit

$$v_i \sim 15 \left( \frac{I_L}{10^{13} \text{ W/cm}^2} \right)^{0.56}$$

- Future Work
  - Amplified Field
     Measurement (B-Dot)
  - RMI + RTI (Early Phase)

$$rac{v_{ ext{lin}}}{k\psi_{0}v_{i}}pprox -0.16 \, { rac{
ho_{2}}{
ho_{1}} = 10^{-5}}_{M_{i}\,=\,5}$$

![](_page_69_Figure_8.jpeg)

## 3. Anisotropic Thermal Conduction

#### GEKKO Experiment in Osaka Matsuo+ PRE 2017

Bottom Line: Anisotropic thermal conduction affects flow dynamics even when the plasma beta is large.

#### Anisotropic thermal conduction affects flow dynamics even when the plasma beta is large.

- Large Plasma Beta: Lorentz force is negligible.
- But the dynamics can be modified by B field via "confinement of plasma thermal energy".

![](_page_71_Figure_3.jpeg)
## Non-uniform heat flow is formed on corrugated planar target in strong B field.

- 1. Modulation on Ablation Side of Target
- 2. Non-uniform Field Distribution Generated by Plasma Flow
- 3. Thermal Energy Kept for Longer Timescale at Stronger Field Region
- 4. Enhance the Modulation







## Non-uniform heat flow enhances the perturbation growth.

- Radiation Magneto-Hydrodynamic Simulation (PINOCO-MHD)
- GEKKO result is in good agreement with the simulation.

Matsuo+ PRE 2017

**B** Parallel

0.0

Without **B** 

0.5

150

Without B

200

**EXP** 



## Summary

- We are investigating the magnetohydrodynamic evolutions of RMI by using both simulations and laser experiments.
- There are 3 interesting features in MHD RMI.
  - 1. A strong magnetic field can reduce the growth of RMI significantly, where the Alfven (Mach) number is the key controlling parameter. Sano+ PRL 2013; Matsuoka+ JNS 2017
  - Turbulent motions driven by RMI can amplify an ambient magnetic field by many orders of magnitude.
    Sano+ ApJ 2012
  - 3. Anisotropic thermal conduction can affect hydrodynamic flows even when the plasma beta is much larger than unity. Matsuo+ PRE 2017