

Project 6

Relativistic MHD simulations using CANS

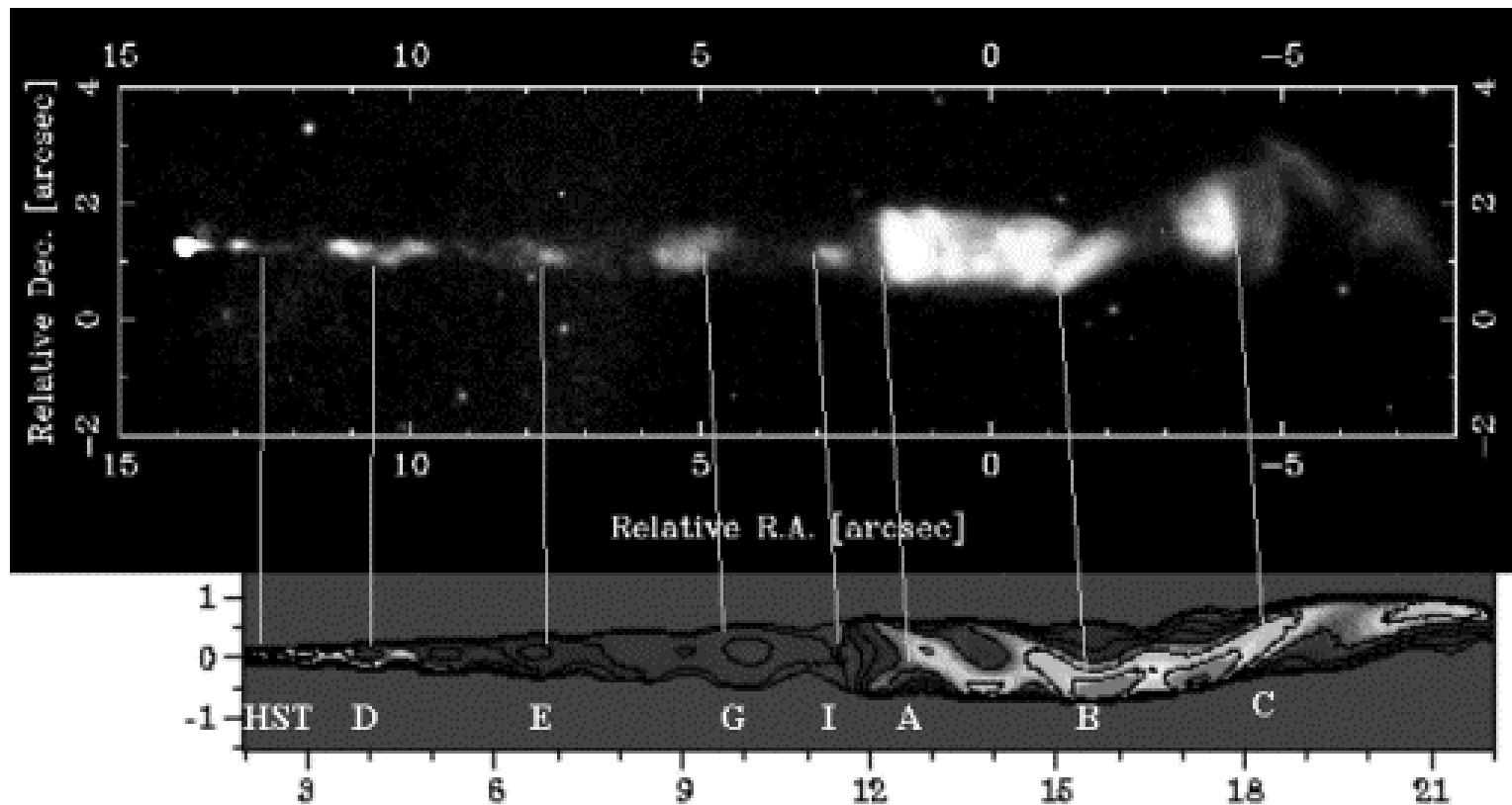
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Introduction: Jet and K-H instability



(Lobanov et al., 2003)

Internal structure of the kiloparsec-scale jet in M87,
possibly related with Kelvin-Helmholtz instability

Special Relativistic Ideal MHD

$$\begin{cases} \frac{\partial D}{\partial t} + \nabla \cdot (D \mathbf{v}) = 0 \\ \frac{\partial \mathbf{P}}{\partial t} + \nabla \cdot \left[p \mathbf{I} + (e + p) \frac{\gamma^2}{c^2} \mathbf{v} \mathbf{v} - \frac{1}{4\pi} \left\{ \mathbf{E} \mathbf{E} + \mathbf{B} \mathbf{B} - \frac{1}{2} (E^2 + B^2) \right\} \right] = 0 \\ \frac{\partial \varepsilon}{\partial t} + \nabla \cdot \left[\{(e + p)\gamma^2 - Dc^2\} \mathbf{v} + \frac{c}{4\pi} (\mathbf{E} \times \mathbf{B}) \right] = 0 \\ \frac{\partial \mathbf{B}}{\partial t} + \nabla \times (c \mathbf{E}) = 0 \end{cases}$$

$$D = \rho\gamma$$

$$\mathbf{P} = (e + p) \frac{\gamma^2}{c^2} \mathbf{v} + \frac{1}{4\pi c} (\mathbf{E} \times \mathbf{B})$$

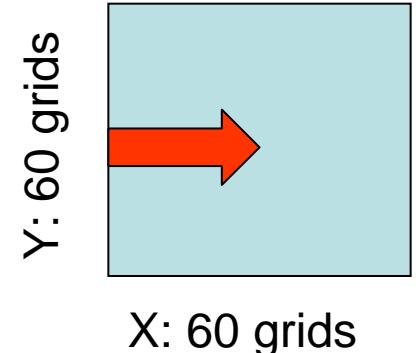
$$\varepsilon = (e + p)\gamma^2 - Dc^2 - p + \frac{1}{8\pi} (E^2 + B^2)$$

$$\mathbf{E} = -\frac{1}{c} \mathbf{v} \times \mathbf{B}$$

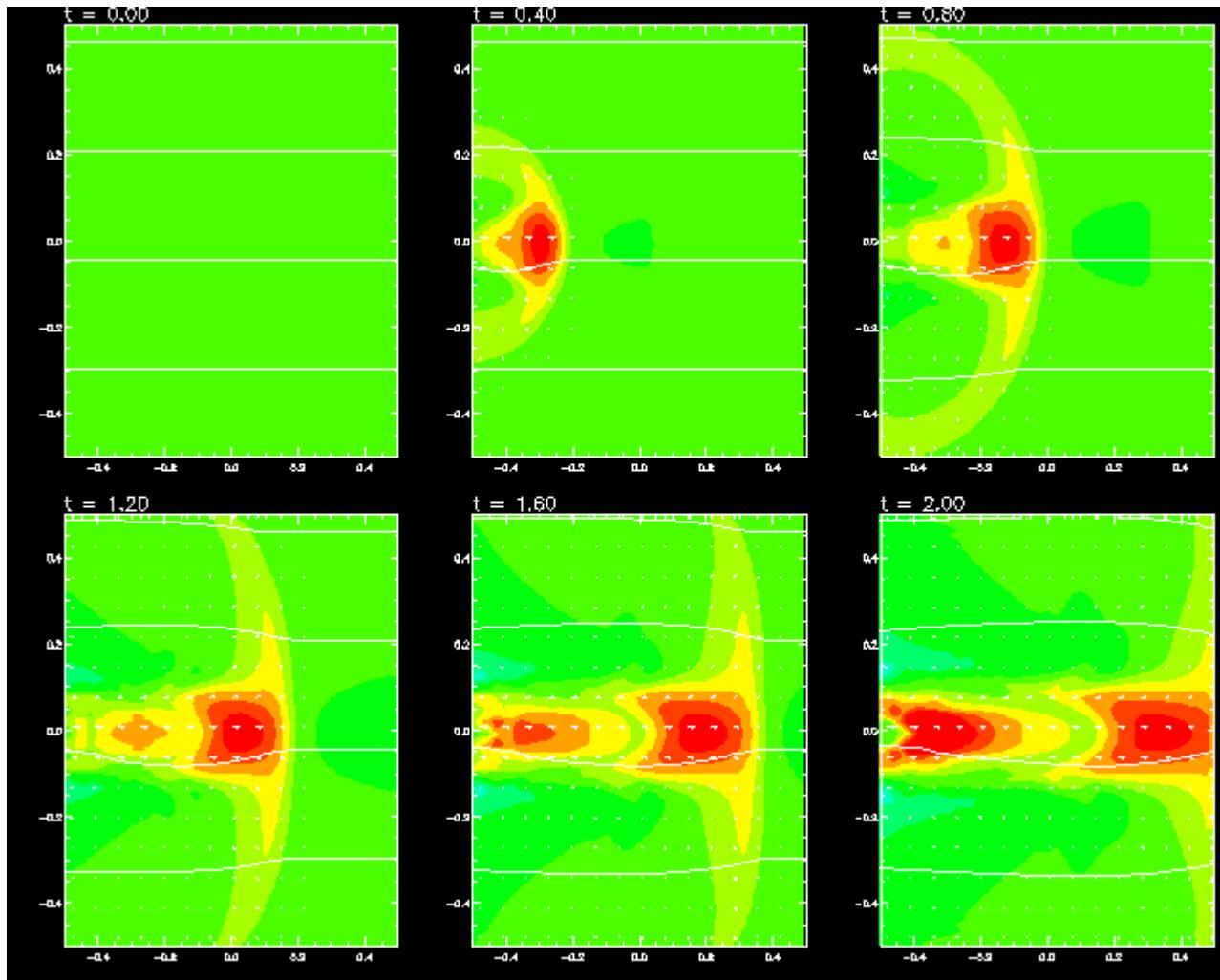
(γ :Lorentz factor, e :thermal energy density)

1. Jet

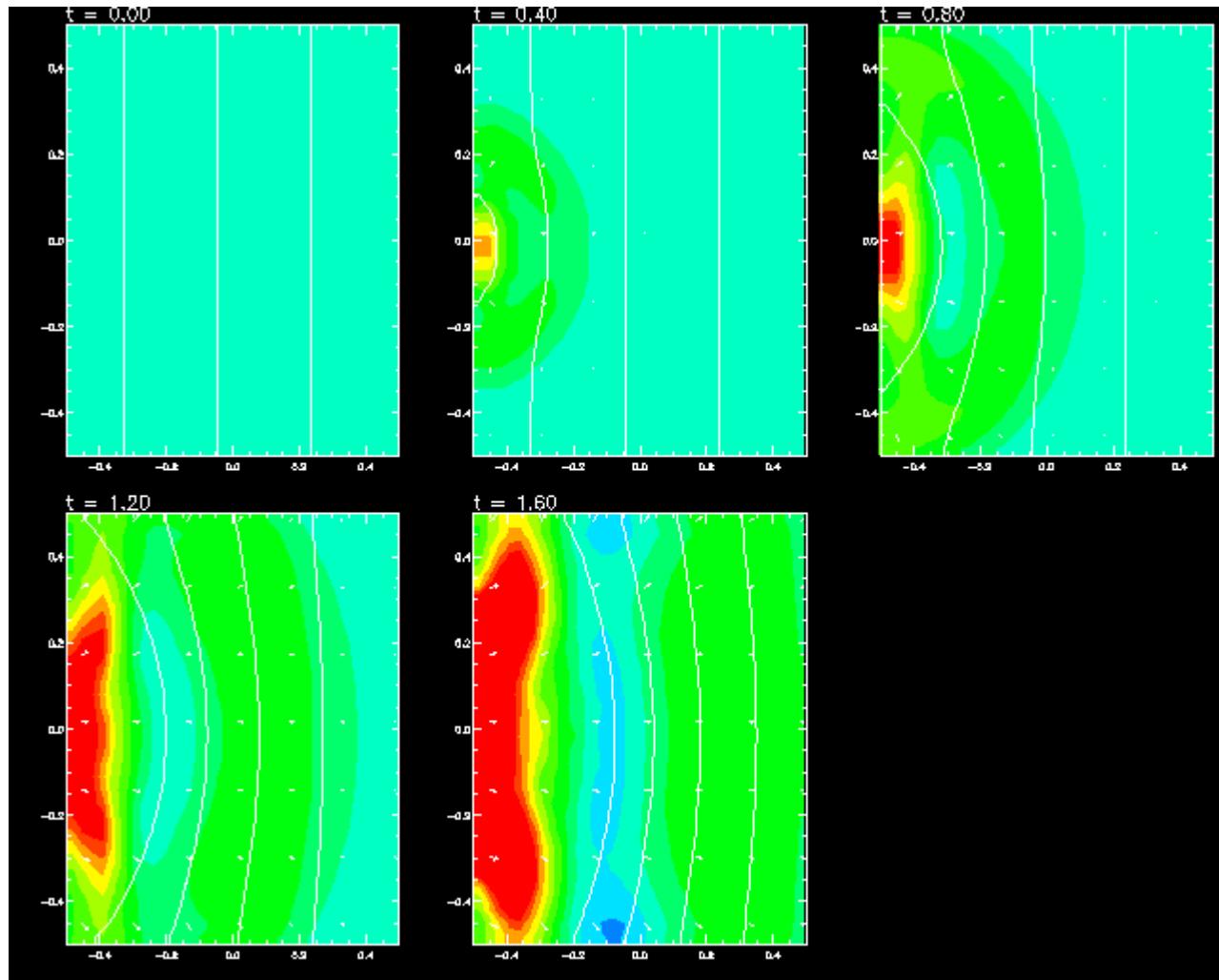
- X: Free, Y: Free
- Continuous plasma Injection of $v_x=0.5$ at $x=0$
- Magnetic field dependence
 - Strong B field
 - Parallel, perpendicular, and oblique B



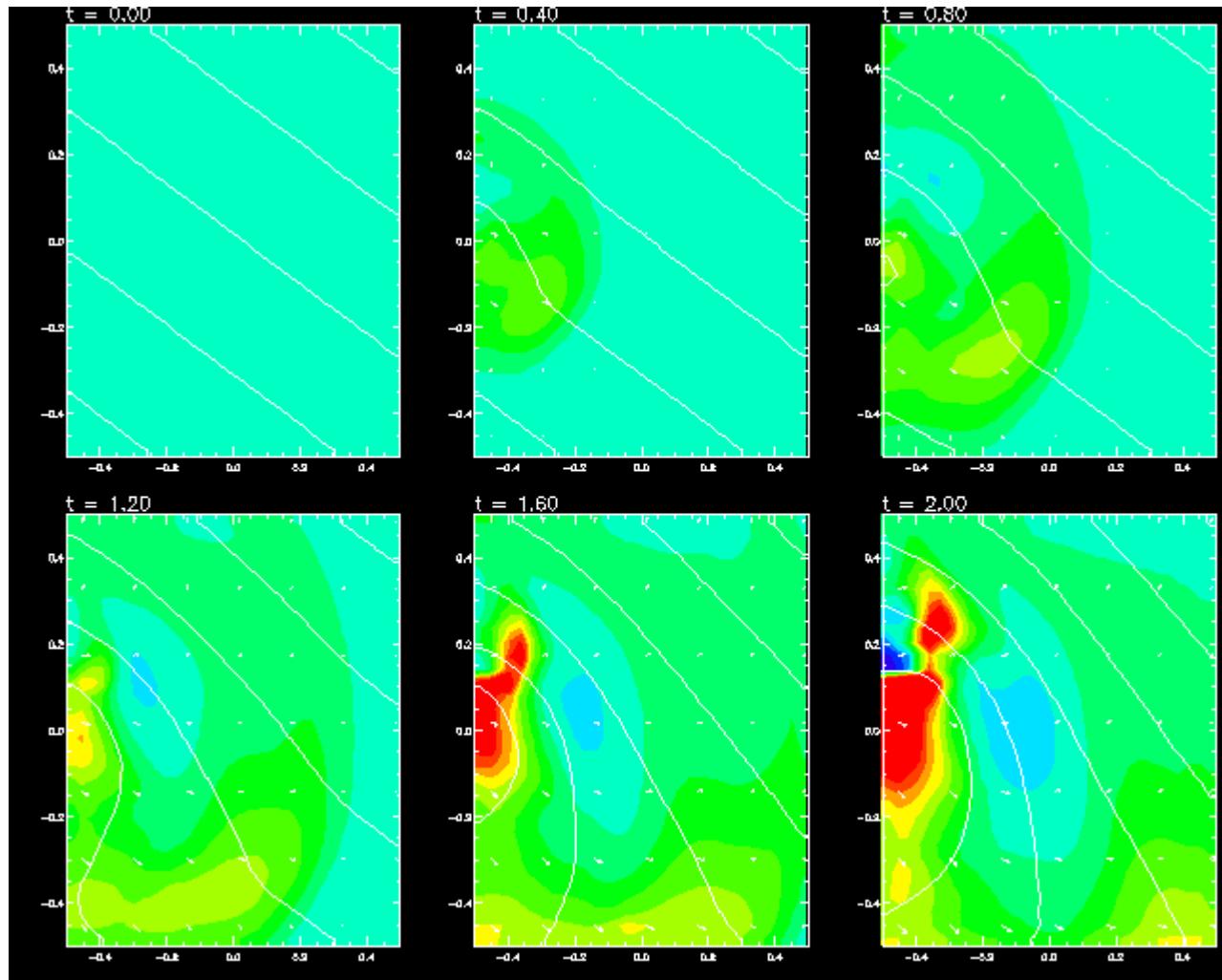
a. Parallel magnetic field



b. Perpendicular magnetic field

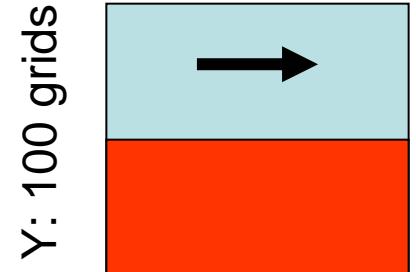


c. Oblique magnetic field

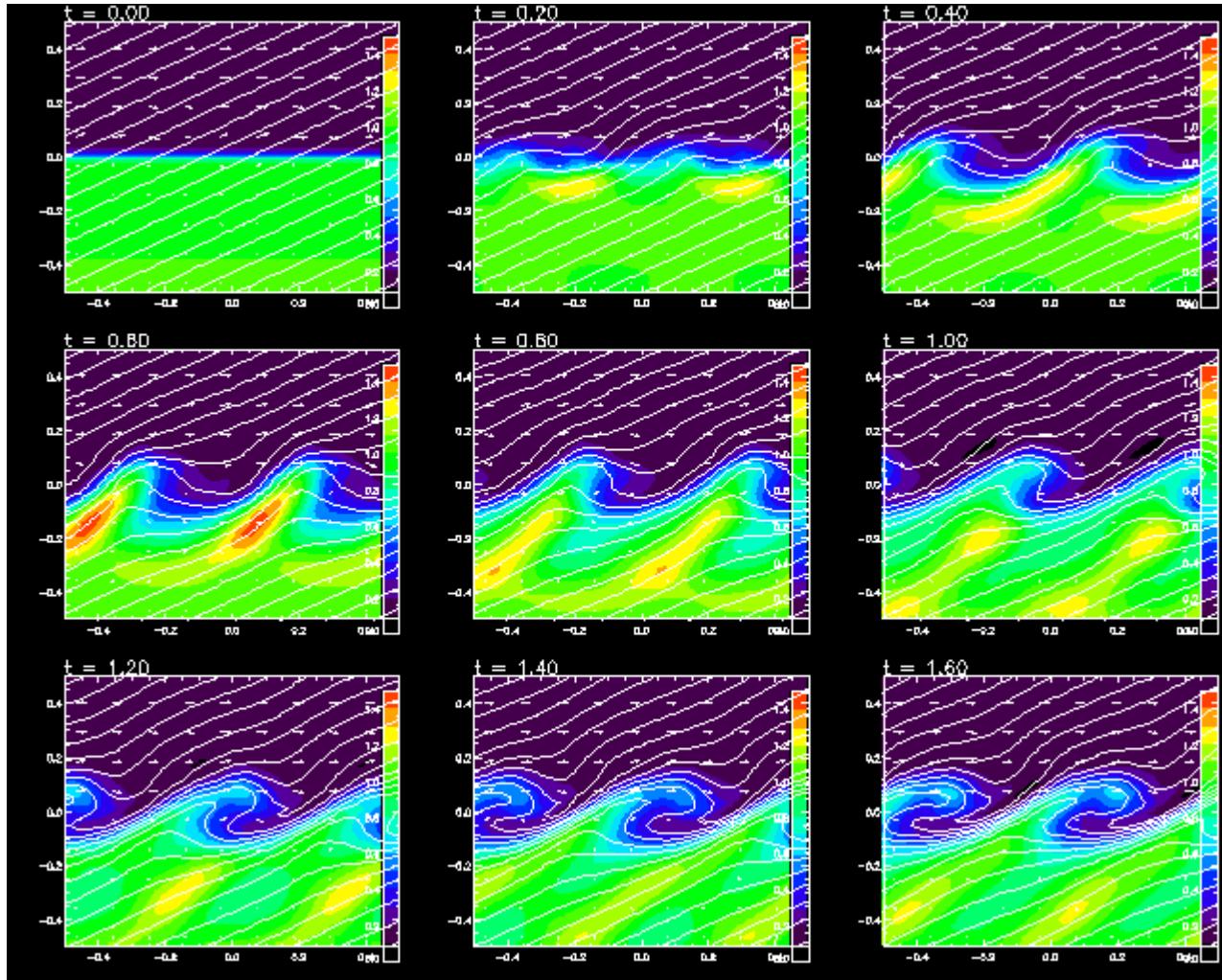


2. K-H Instability

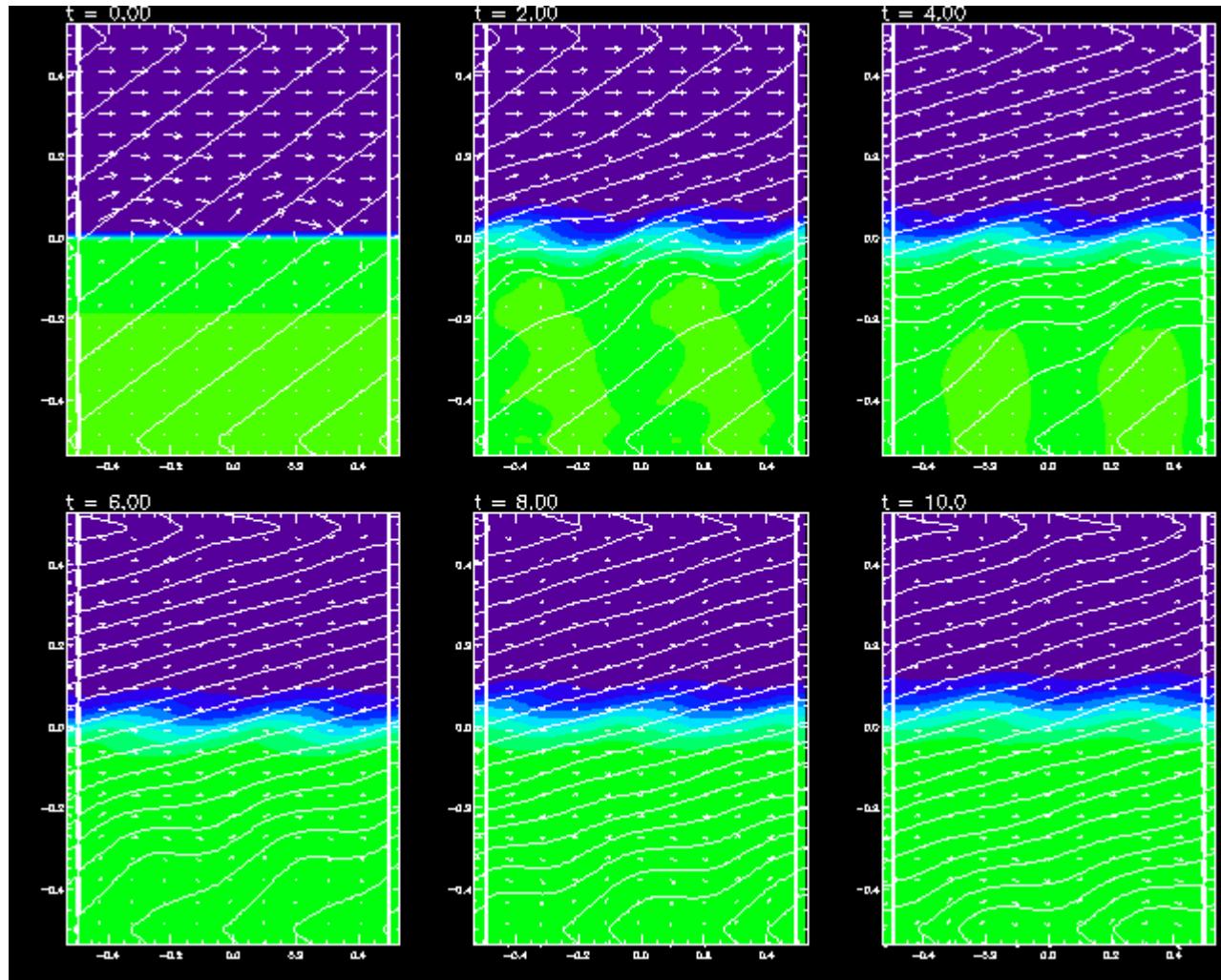
- X: Periodic, Y: Symmetric
- Pressure-balanced layers with velocity shear: perturbation applied
- MHD and relativistic MHD
 - Parallel, perpendicular, and oblique B
- Parametric survey
 - Velocity shear dependence of growth rate



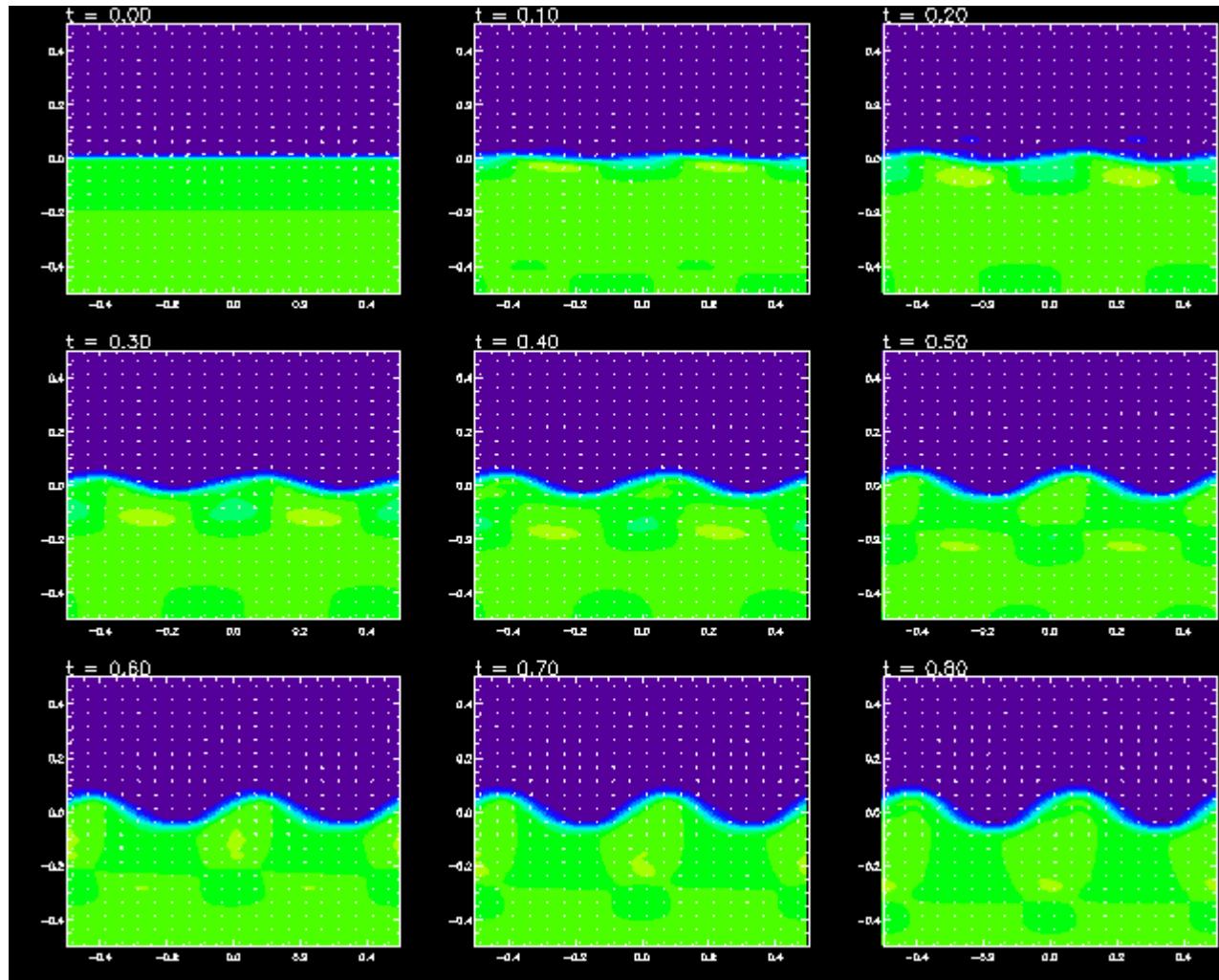
Relativistic MHD



MHD

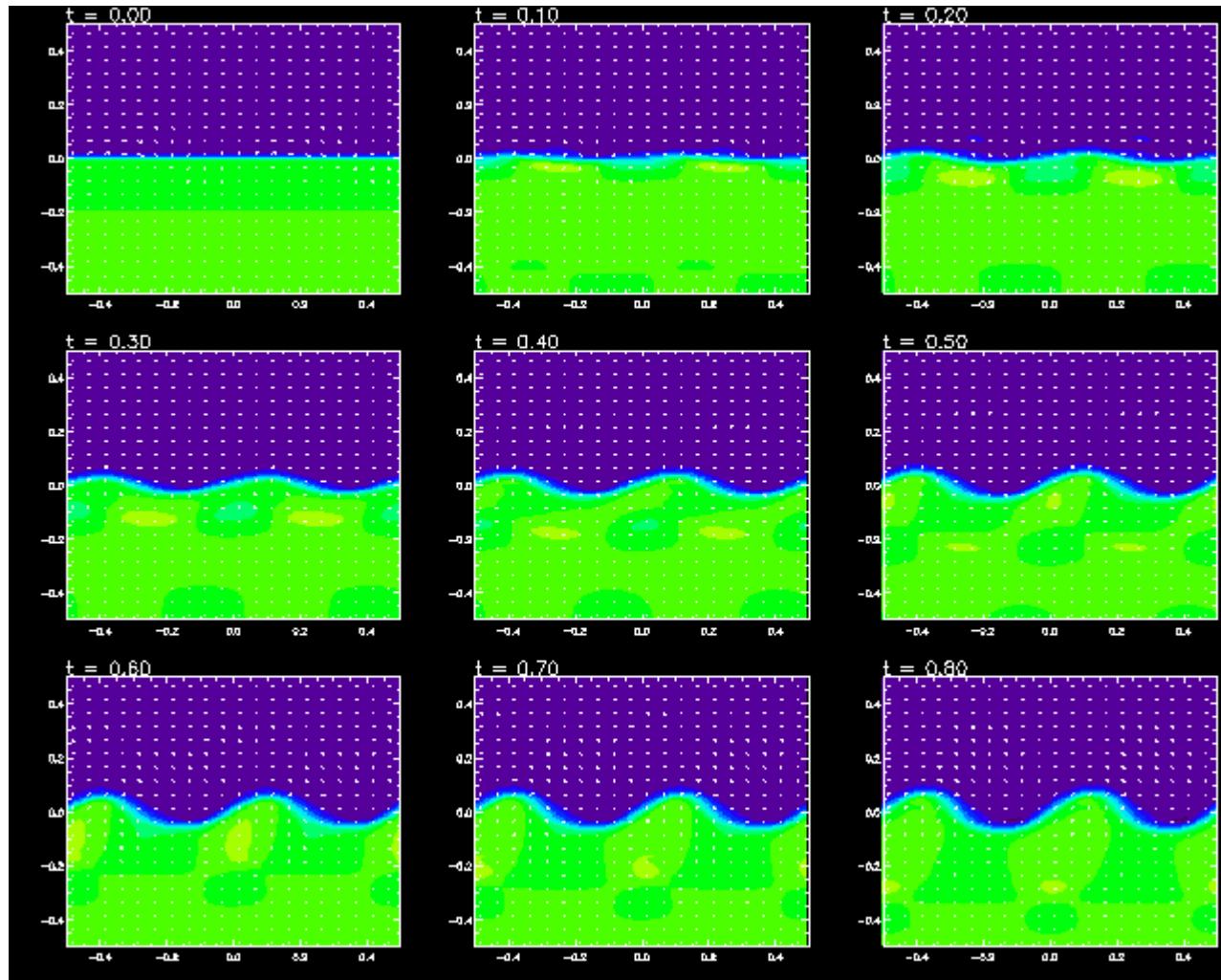


$Vx=0.0$



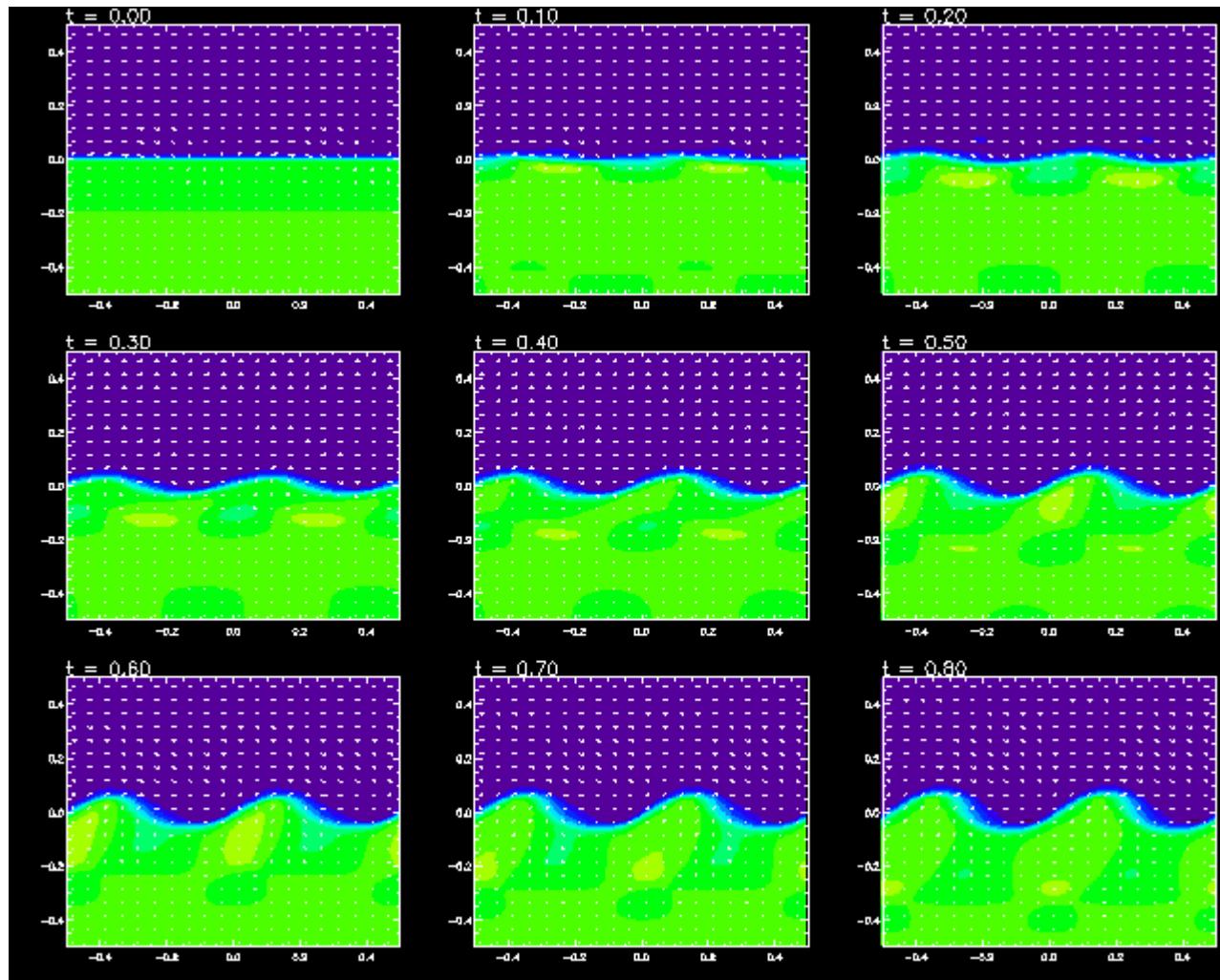
Velocity shear dependence of KHI growth rate

$Vx=0.1$



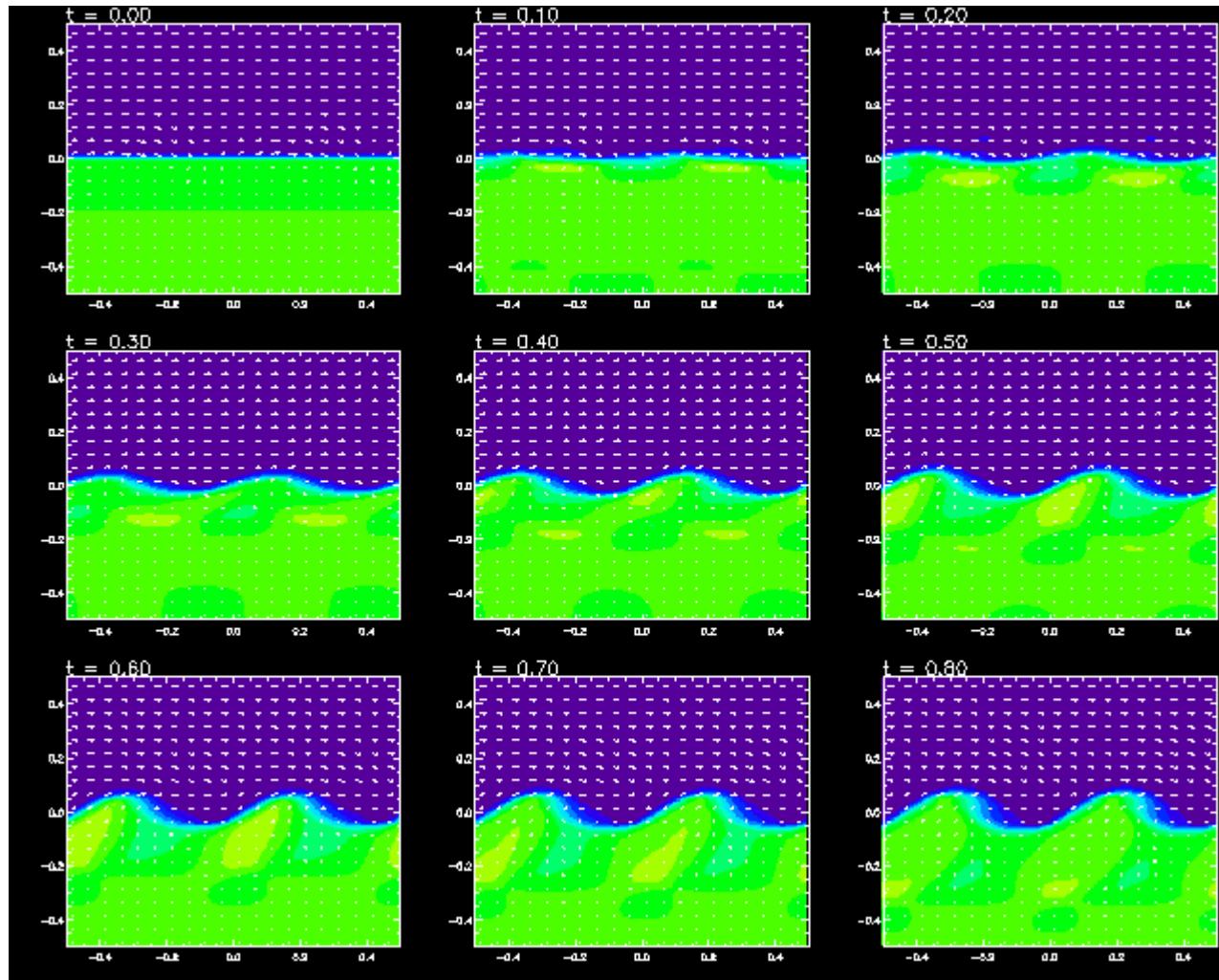
Velocity shear dependence of KHI growth rate

$V_x=0.2$



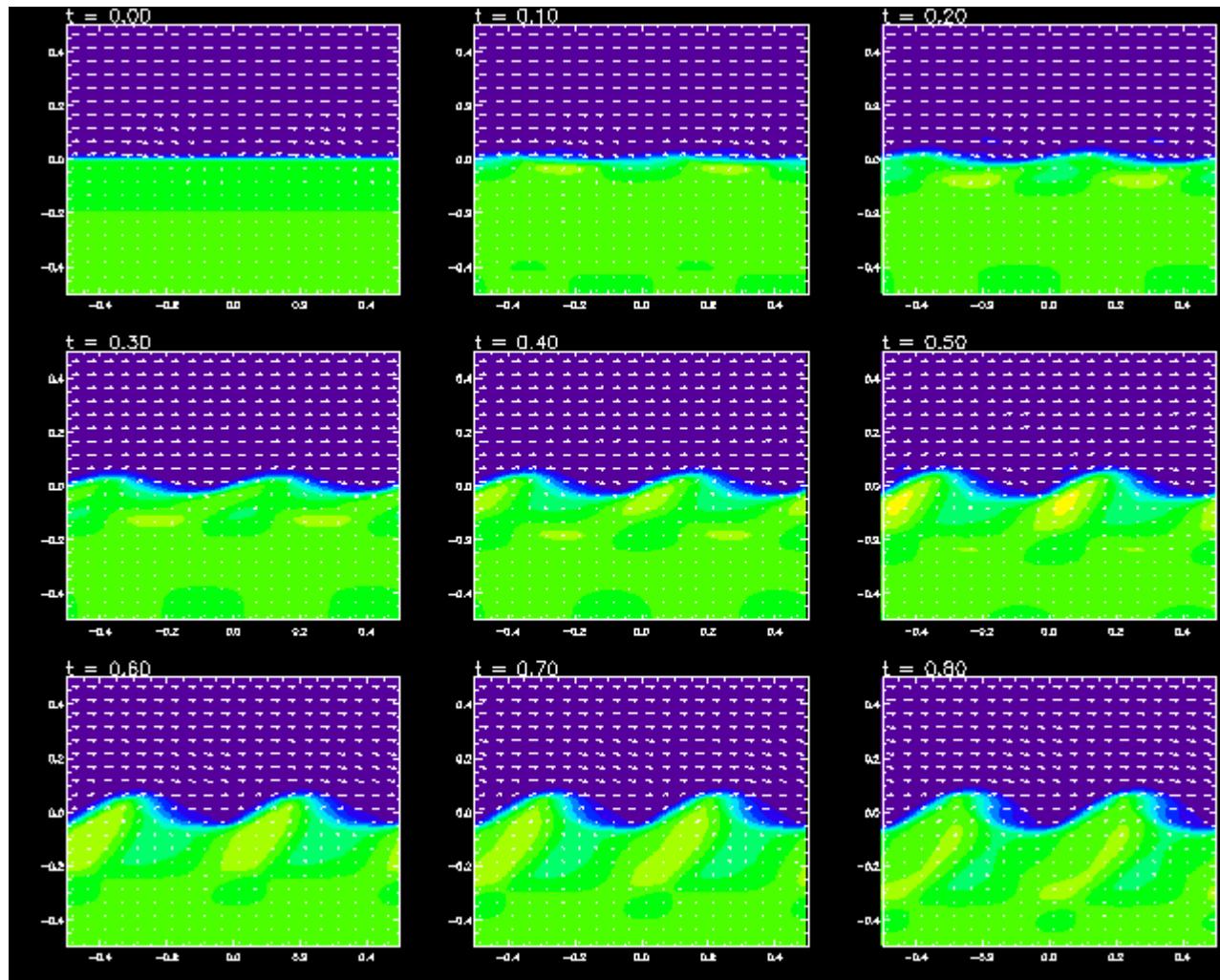
Velocity shear dependence of KHI growth rate

$Vx=0.3$



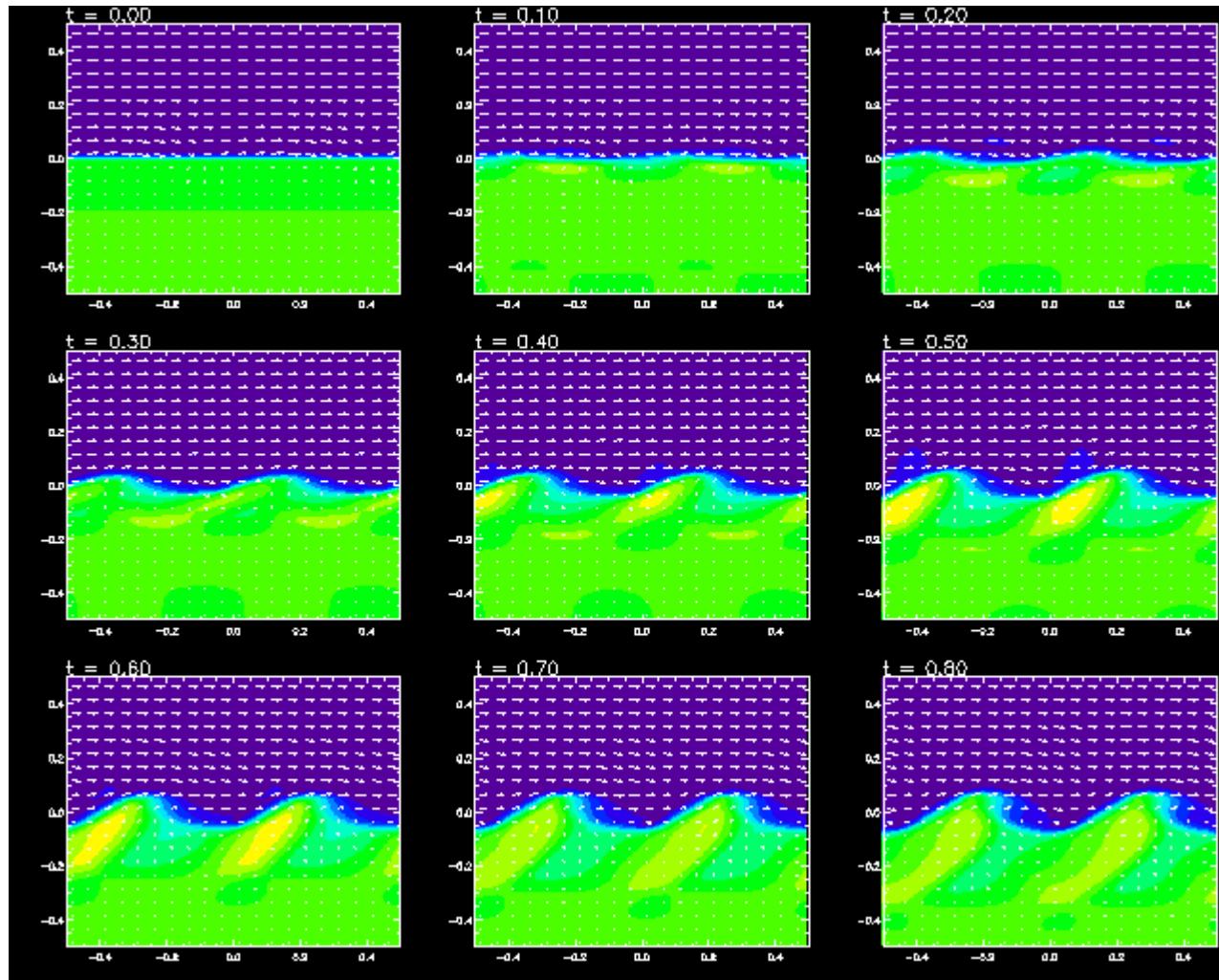
Velocity shear dependence of KHI growth rate

$Vx=0.4$



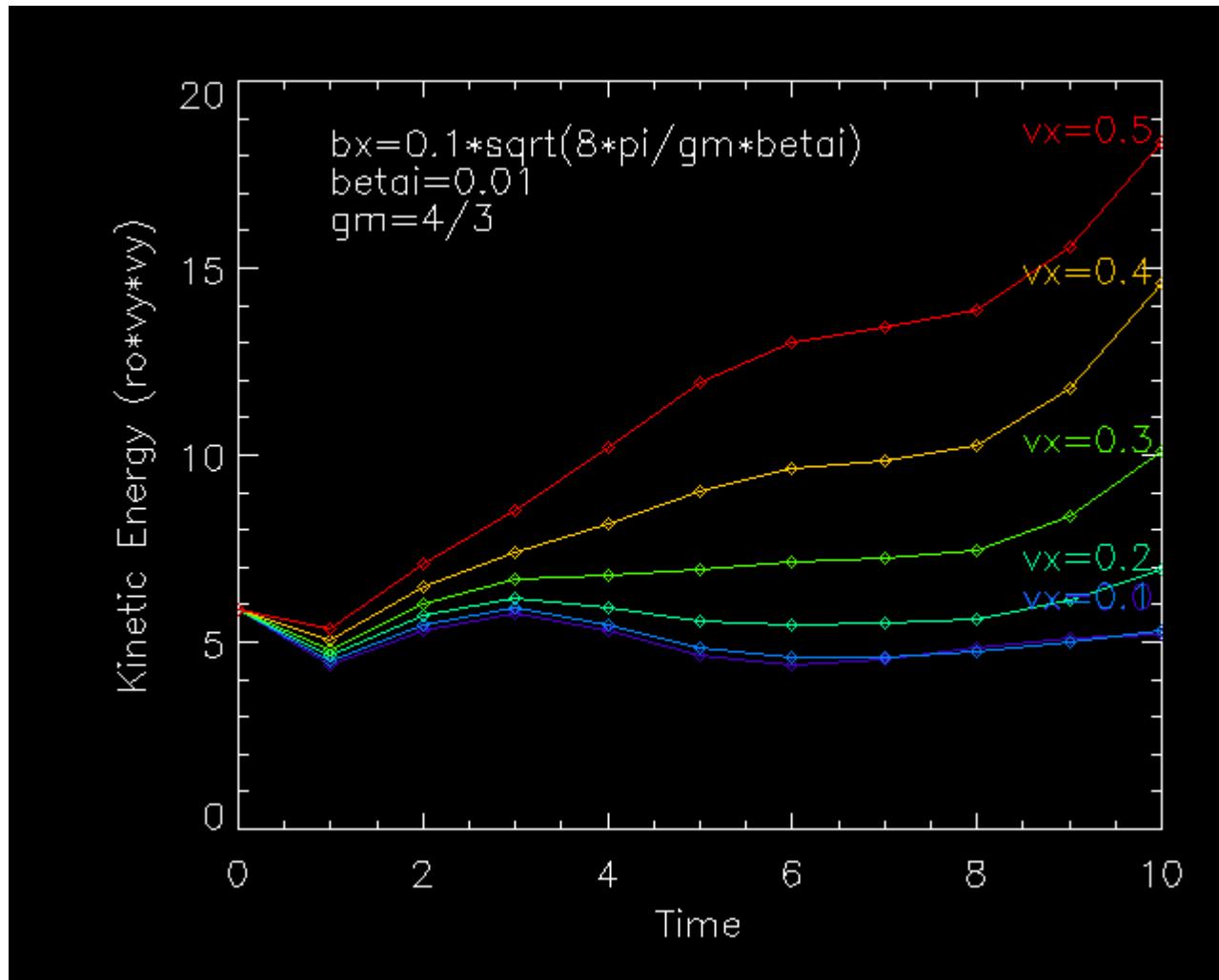
Velocity shear dependence of KHI growth rate

$V_x=0.5$



Velocity shear dependence of KHI growth rate

KHI growth



Conclusions

- We performed relativistic MHD simulations using CANS 2D
- Jet
 - Morphology of Jet depending on B field
- Kelvin-Helmholtz Instabilities
 - Comparison with MHD
 - B field dependence
 - Parametric survey
 - Velocity shear dependence

